

# Enzo Lectures

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	Morning	Afternoon
Mon.	Introduction to Enzo	
Tue.	1. Setting Up and Running Enzo 2. Enzo Projects	Introduction to YT
Wed.	<b>Basic Enzo Algorithms</b>	<b>Lab session</b>
Thu.	Applications to First Stars, First Galaxies, and Reionization	Lab session
Fri.	What's New in Enzo 2.0?	Q & A

# Basic Enzo Algorithms

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# Topics

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## I. Hydrodynamics

- ▶ PPM
- ▶ ZEUS

## II. AMR

- ▶ Timestepping
- ▶ Projection
- ▶ Flux correction

## III. Gravity

- ▶ Root grid
- ▶ Subgrids

## IV. Particles

## V. Chemistry & Cooling

- ▶ Multispecies
- 





# I. Hydrodynamics

Show PPM movies

# Fluid Equations - grid::SolveHydroEquations

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Mass conservation  $\frac{\partial \rho}{\partial t} + \frac{1}{a} \mathbf{v} \cdot \nabla \rho = -\frac{1}{a} \rho \nabla \cdot \mathbf{v}$

Momentum conservation  $\frac{\partial \mathbf{v}}{\partial t} + \frac{1}{a} (\mathbf{v} \cdot \nabla) \mathbf{v} = -\frac{\dot{a}}{a} \mathbf{v} - \frac{1}{a \rho} \nabla p - \frac{1}{a} \nabla \phi,$

Energy conservation  $\frac{\partial E}{\partial t} + \frac{1}{a} \mathbf{v} \cdot \nabla E = -\frac{\dot{a}}{a} (3 \frac{p}{\rho} + \mathbf{v}^2) - \frac{1}{a \rho} \nabla \cdot (p \mathbf{v}) - \frac{1}{a} \mathbf{v} \cdot \nabla \phi + \Gamma - \Lambda.$

$$E = e + \frac{1}{2} \mathbf{v}^2,$$

Ideal Gas EOS  $e = p / [(\gamma - 1) \rho],$

Self-gravity  $\nabla^2 \phi = \frac{4\pi G}{a} (\rho_{total} - \rho_0).$

Field names: Density, Pressure, TotalEnergy, InternalEnergy,  
Velocity1, Velocity2, Velocity3

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# grid class: accessing the fields – grid.h

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- ▶ In grid class:
  - ▶ BaryonFields[] – array of pointers to each field
    - ▶ Fortran (row-major) ordering within each field
  - ▶ GridRank – dimensionality of problem
  - ▶ GridDimensions[] – dimensions of this grid
  - ▶ GridStartIndex[] – Index of first “active” cell (usually 3)
    - ▶ First (and last) three cells are ghost or boundary zones

```
int DensNum = FindField(Density, FieldType, NumberOfBaryonFields);  
int Vel1Num = FindField(Velocity1, FieldType, NumberOfBaryonFields);
```

```
for (k = GridStartIndex[2]; k <= GridEndIndex[2]; k++) {  
  for (j = GridStartIndex[1]; j <= GridEndIndex[1]; j++) {  
    for (i = GridStartIndex[0]; i <= GridEndIndex[0]; i++) {  
      BaryonField[Vel1Num][GINDEX(i,j,k)] *= BaryonField[DensNum][GINDEX(i,j,k)];  
    }  
  }  
}
```

---



# Enzo file name convention

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- ▶ **General C++ routines:**

- ▶ Routine name: EvolveLevel(...)
- ▶ In file: EvolveLevel.C
- ▶ One routine per file!

- ▶ **grid methods:**

- ▶ Routine name: grid::MyName(...)
- ▶ In file: Grid\_MyName.C

- ▶ **Fortran routines:**

- ▶ Routine name: intvar(...)
- ▶ In file: intvar.src
  - ▶ .src is used because routine is fed first through C preprocessor



# PPM Solver: grid::SolvePPM\_DE

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- ▶ HydroMethod = 0
- ▶ PPM: e.g. mass conservation equation

- ▶ Flux conservative form:

$$\frac{\partial \rho}{\partial t} + \frac{\partial \rho v}{\partial x} = 0 \quad \rho_j^n = \rho(x_j, t^n)$$

Mass flux across  $j+1/2$  boundary

- ▶ In discrete form:

$$\rho_j^{n+1} = \rho_j^n + \Delta t \left( \frac{\bar{\rho}_{j+1/2} \bar{v}_{j+1/2} - \bar{\rho}_{j-1/2} \bar{v}_{j-1/2}}{\Delta x_j} \right)$$

- ▶ How to compute mass flux?
- ▶ **Note: multi-dimensions handled by operating splitting**
  - ▶ grid::xEulerSweep.C, grid::yEulerSweep.C, grid::zEulerSweep.C





# Grid::SolvePPM\_DE

---

```
// Update in x-direction
for (k = 0; k < GridDimension[2]; k++) {
    if (this->xEulerSweep(k, NumberOfSubgrids, SubgridFluxes,
        GridGlobalStart, CellWidthTemp, GravityOn,
        NumberOfColours, colnum) == FAIL) {
        fprintf(stderr, "Error in xEulerSweep. k = %d\n", k);
        ENZO_FAIL("");
    }
} // ENDFOR k

// Update in y-direction
for (i = 0; i < GridDimension[0]; i++) {
    if (this->yEulerSweep(i, NumberOfSubgrids, SubgridFluxes,
        GridGlobalStart, CellWidthTemp, GravityOn,
        NumberOfColours, colnum) == FAIL) {
        fprintf(stderr, "Error in yEulerSweep. i = %d\n", i);
        ENZO_FAIL("");
    }
} // ENDFOR i
```

---



## PPM: 1D hydro update: `grid::xEulerSweep`

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- ▶ Copy 2D slice out of cube
- ▶ Compute pressure on slice (`pgas2d`)
- ▶ Calculate diffusion/steepening coefficients (`calcdiss`)
- ▶ Compute Left and Right states on each cell edge (`inteuler`)
- ▶ Solve Riemann problem at each cell edge (`twoshock`)
- ▶ Compute fluxes of conserved quantities at each cell edge (`euler`)
- ▶ Save fluxes for future use
- ▶ Return slice to cube



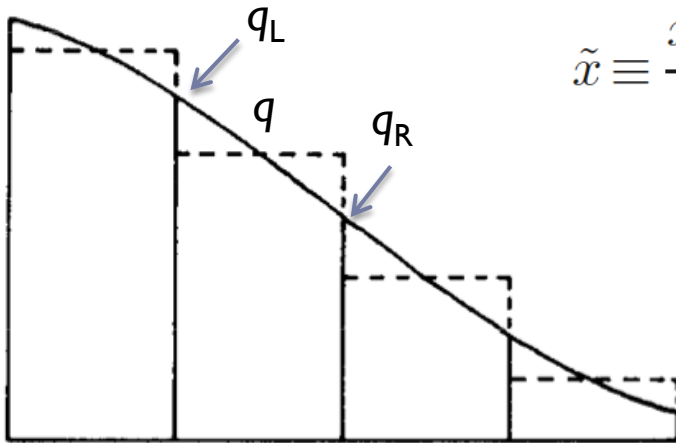
# PPM: reconstruction: inteuler

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- ▶ Piecewise parabolic representation:

$$q_j(x) = q_{L,j} + \tilde{x}(\Delta q_j + q_{6,j}(1 - \tilde{x})),$$

$$\tilde{x} \equiv \frac{x - x_{j-1/2}}{\Delta x_j}, \quad x_{j-1/2} \leq x \leq x_{j+1/2}.$$



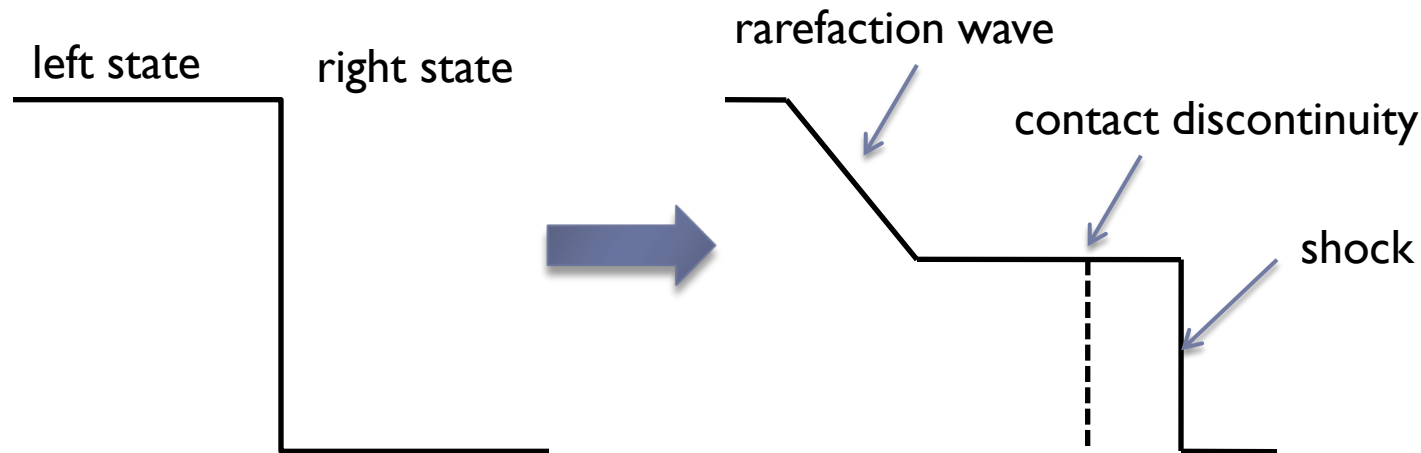
- ▶ Coefficients ( $\Delta q$  and  $q_6$ ) computed with mean  $q$  and  $q_L, q_R$ .
  - ▶ For smooth flow (like shown above), this is fine, but can cause a problem for discontinuities (e.g. shocks)
  - ▶  $q_L, q_R$  are modified to ensure monotonicity (no *new* extrema)
- 



# PPM: Godunov method: twoshock

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- ▶ To compute flux at cell boundary, take two initial constant states and then solve Riemann problem at interface

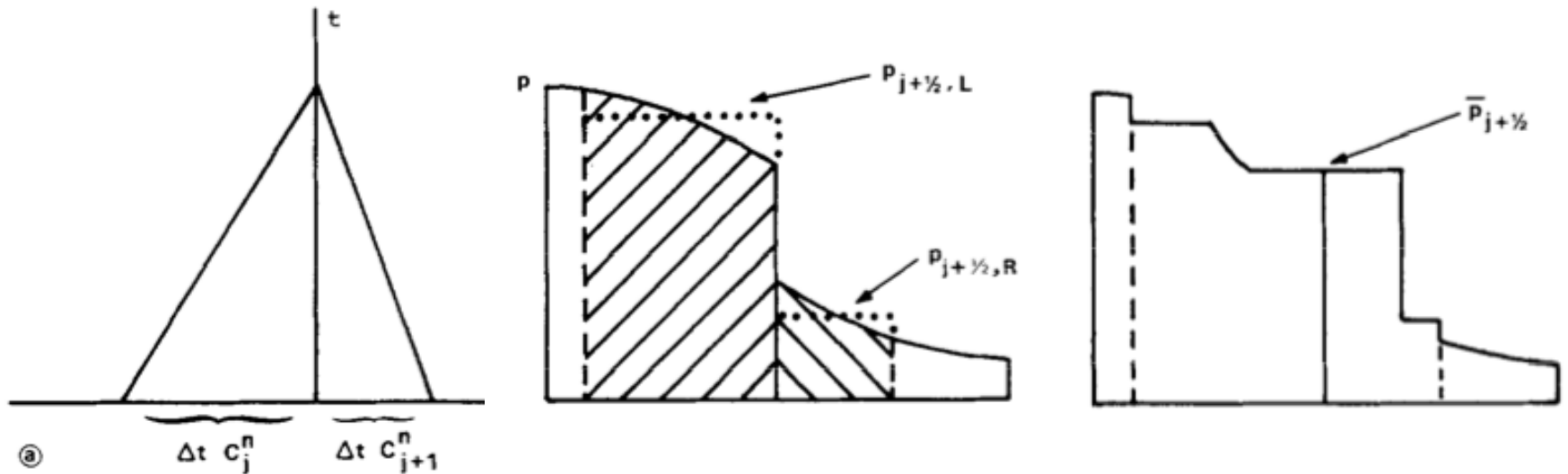


- ▶ Given solution, can compute flux across boundary
  - ▶ Advantage: correctly satisfies jump conditions for shock
- 



# PPM: Godunov method: inteuler, twoshock

- ▶ For PPM, compute left and right states by averaging over characteristic region (causal region for time step  $\Delta t$ )

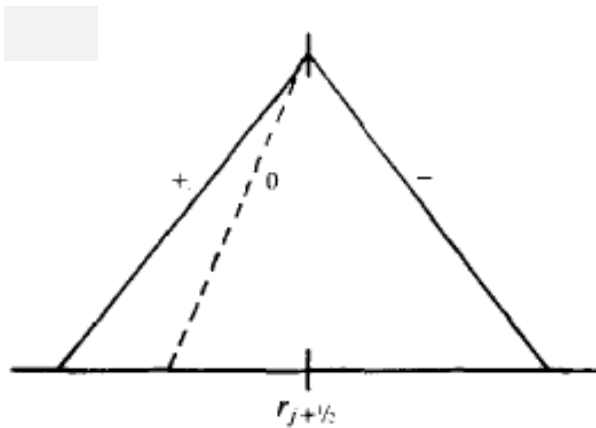


- ▶ Average left and right regions become constant regions to be feed into Riemann solver (twoshock).

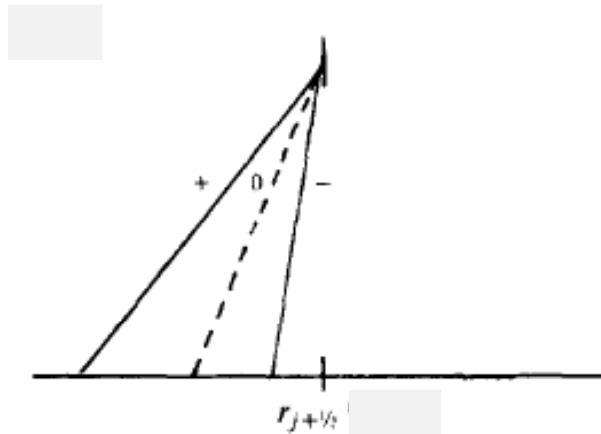
# PPM: Eulerian corrections: euler

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- ▶ Eulerian case more complicated because cell edge is fixed.
  - ▶ Characteristic region for fixed cell more complicated:



SUBSONIC CASE



SUPERSONIC CASE

- ▶ Note that solution is not known ahead of time so two-step procedure is used (see Collela & Woodward 1984 for details)



# Difficulty with very high Mach flows

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- ▶ PPM is flux conservative so natural variables are mass, momentum, *total* energy

- ▶ Internal energy ( $e$ ) computed from total energy ( $E$ ):

$$e = E - \frac{1}{2}v^2$$

- ▶ Problem can arise in very high Mach flows when  $E \gg e$ 
  - ▶  $e$  is difference between two large numbers
- ▶ Not important for flow dynamics since  $p$  is negligible
  - ▶ But can cause problems if we want accurate temperatures since  $T \propto e$



# Dual Energy Formalism:

grid::ComputePressureDualEnergyFormalism

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- ▶ Solution: Also evolve equation for internal energy:

$$\frac{\partial e}{\partial t} + \frac{1}{a} \mathbf{v} \cdot \nabla e = \frac{p}{a\rho} \nabla \cdot \mathbf{v}$$

- ▶ Select energy to use depending on ratio  $e/E$ :

$$p = \begin{cases} \rho(\gamma - 1)(E - \mathbf{v}^2/2), & (E - \mathbf{v}^2/2)/E > \eta_1; \\ \rho(\gamma - 1)e, & (E - \mathbf{v}^2/2)/E < \eta_1. \end{cases}$$

- ▶ Select with DualEnergyFormalism = 1
- ▶ Use when  $v/c_s > \sim 20$
- ▶ Q: Why not just use  $e$ ?
  - ▶ A: Equation for  $e$  is not in conservative form (source term).
  - ▶ Source term in internal energy equation causes diffusion





# Zeus Solver: grid::ZeusSolver

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- ▶ Traditional finite difference method

- ▶ Artificial viscosity (see Stone & Norman 1992)

- ▶ HydroMethod = 2

- ▶ Source step: ZeusSource

- ▶ Pressure (and gravity) update: 
$$v_j^{n+a} = v_j^n - \frac{\Delta t}{\Delta x_j} \frac{p_j^n - p_{j-1}^n}{(\rho_j^n + \rho_{j-1}^n)/2}$$

- ▶ Artificial viscosity: 
$$v_j^{n+b} = v_j^{n+a} - \frac{\Delta t}{\Delta x_j} \frac{q_j^{n+a} - q_{j-1}^{n+a}}{(\rho_j^n + \rho_{j-1}^n)/2}$$
$$q_j = \begin{cases} Q_{AV} \rho_j (v_{j+1} - v_j)^2 & \text{if } (v_{j+1} - v_j) < 0 \\ 0 & \text{otherwise} \end{cases}$$

- ▶ Compression heating: 
$$e_j^{n+c} = e_j^{n+b} \left( \frac{1 - (\Delta t/2)(\gamma - 1)(\nabla \cdot \mathbf{v})_j}{1 + (\Delta t/2)(\gamma - 1)(\nabla \cdot \mathbf{v})_j} \right)$$



# Zeus Solver: grid::ZeusSolver

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- ▶ Transport step: Zeus\_xTransport

e.g. 
$$\rho_j^{n+d} = \rho_j^n - \frac{\Delta t}{\Delta x} (v_{j+1/2}^{n+c} \rho_{j+1/2}^* - v_{j-1/2}^{n+c} \rho_{j-1/2}^*)$$

- ▶ Note conservative form (transport part preserves mass)
- ▶ Note  $v_{j+1/2}$  is face-centered so is really at cell-edge, but density needs to be interpolated. Zeus uses an upwinded van Leer (linear) interpolation:

$$q_j(x) = q_{L,j} + \tilde{x}(\Delta q_j)$$

- ▶ Similarly for momentum and energy (and y and z)
  - ▶ Zeus\_yTransport, Zeus\_zTransport



# Zeus Solver: `grid::ZeusSolver`

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- ▶ PPM is more accurate, slower but Zeus is faster and more robust.
  - ▶ PPM often fails (“ $dnu < 0$ ” error) when fast cooling generates large density gradients.
  - ▶ Try out new hydro solvers in Enzo 2.0!
- ▶ **Implementation differences with PPM:**
  - ▶ Internal energy equation only
    - ▶ In code, TotalEnergy field is really internal energy (ugh!)
  - ▶ Velocities are face-centered
    - ▶ `BaryonField[Vel1Num][GINDEX(i,j,k)]` really “lives” at  $i-1/2$

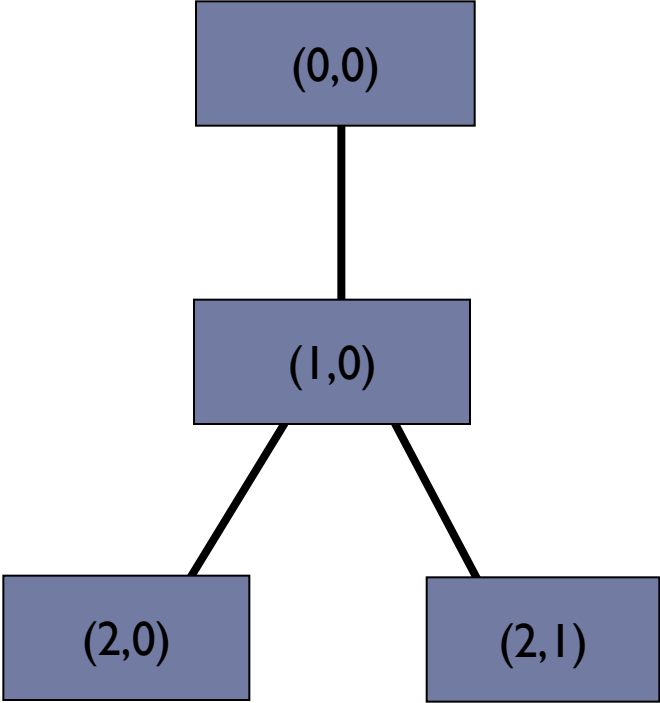
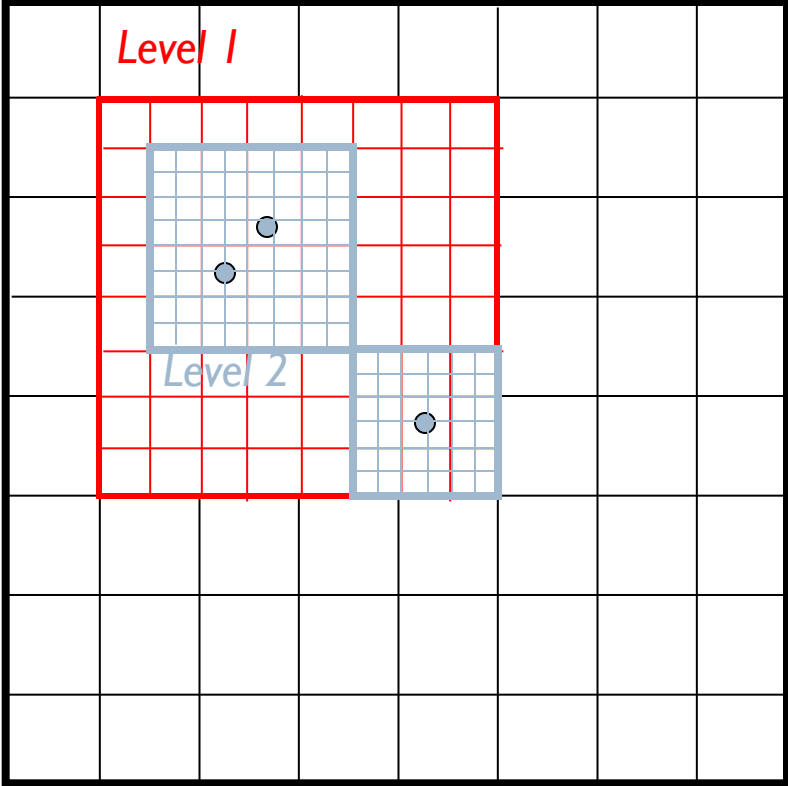




## II. Block Structured AMR

# Grid Hierarchy Data Structure

Level 0



# AMR: EvolveHierarchy

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- ▶ Root grid  $N \times N \times N$ , so  $\Delta x = \text{DomainWidth}/N$
- ▶ Level  $L$  defined so  $\Delta x = \text{DomainWidth}/(N^{2^L})$
- ▶ Starting with level 0, grid advanced by  $\Delta t$ 
  - ▶ Main loop of EvolveHierarchy looks (roughly) like this:

```
InitializeHierarchy
While (Time < StopTime)
begin
    dt = ComputeTimeStep(0)
    EvolveLevel(0, dt)
    Time = Time + dt
    CheckForOutput(Time)
end
```

- ▶ EvolveLevel does the heavy lifting
- 



# Time Step: `grid::ComputeTimeStep`

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- ▶ Timestep on level L is minimum of constraints over all level L grids:

$$\Delta t_{hydro} = \min \left( \kappa_{hydro} \frac{a \Delta x}{c_s + |v_x|} \right)_L \quad \kappa_{hydro} \text{ CourantSafetyFactor}$$

$$\Delta t_{dm} = \min \left( \kappa_{dm} \frac{a \Delta x}{v_{dm,x}} \right)_L, \quad \kappa_{dm} \text{ ParticleCourantSafetyFactor}$$

$$\Delta t_{exp} = f_{exp} \left( \frac{a}{\dot{a}} \right), \quad f_{exp} \text{ MaximumExpansionFactor}$$

$$\Delta t_{accel} = \min \left( \sqrt{\frac{\Delta x}{\vec{g}}} \right)_L$$

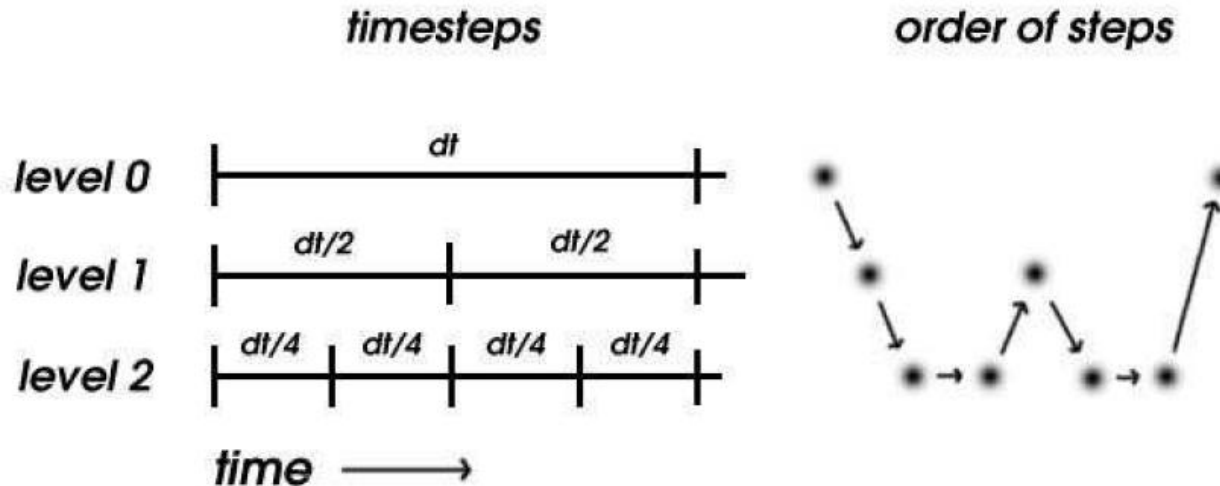
- ▶ + others (e.g. MHD, FLD, etc.)



# AMR: EvolveLevel

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- ▶ Levels advanced as follows:



- ▶ Timesteps may not be integer ratios
  - ▶ (Diagram assumes Courant condition dominates and sound speed is constant so:  $dt \propto \Delta x$ )
- ▶ This algorithm is defined in EvolveLevel





# Advance grids on level: EvolveLevel

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- ▶ The logic of EvolveLevel is given (roughly) as:

```
EvolveLevel(level)
begin
  SetBoundaryValues
  while (Time < ParentTime)
  begin
    dt = ComputeTimeStep(level)
    SolveHydroEquations(dt)
    Time = Time + dt
    SetBoundaryValues
    recursive → EvolveLevel(level+1, dt)
    FluxCorrection
    Projection
    RebuildHierarchy(level+1)
  end
end
end
```

Already talked about this.

Next, we'll talk about these



# BC's: SetBoundaryConditions

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- ▶ **Setting “ghost” zones around outside of domain**
  - ▶ `grid::SetExternalBoundaryValues`
  - ▶ **Choices:** reflecting, outflow, inflow, periodic
  - ▶ Only applied to level 0 grids (except periodic)
- ▶ **Otherwise, two step procedure:**
  - ▶ Interpolate ghost (boundary) zones from level L-1 grid
    - ▶ `grid::InterpolateBoundaryFromParent`
      - Linear interpolation in time (OldBaryonFields)
      - Spatial interpolation controlled by `InterpolationMethod`
        - `SecondOrderA` recommended, default (3D, linear in space, monotonic)
  - ▶ Copy ghost zones from sibling grids
    - ▶ `grid::CheckForOverlap` and `grid::CopyZonesFromGrid`

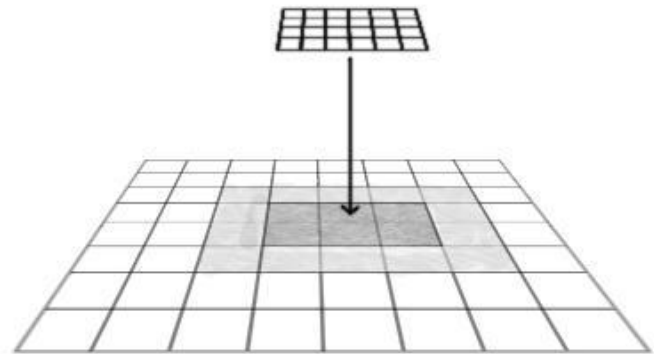


# Projection: `grid::ProjectSolutionToParentGrid`

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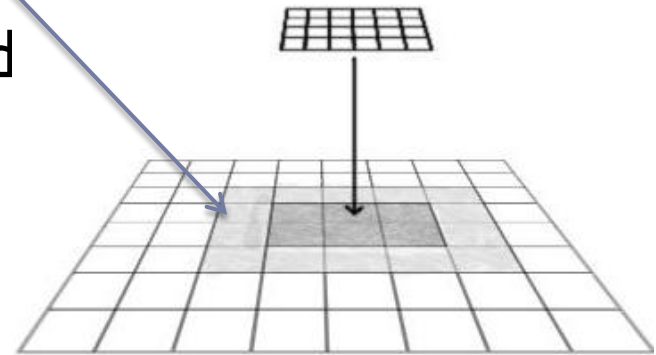
- ▶ **Structured AMR produces redundancy:**
  - ▶ coarse and fine grids cover same region
- ▶ **Need to restore consistency**
- ▶ **Correct coarse cells once grids have all reach the same time:**

$$q^{\text{coarse}} = r^{-d} \sum q_{i,j,k}^{\text{fine}}$$



# Flux Correction: `grid::CorrectForRefinedFluxes`

- ▶ Mismatch of fluxes occurs around boundary of fine grids
  - ▶ Coarse cell just outside boundary used coarse fluxes but coarse cell inside used fine fluxes
- ▶ Both fine and coarse fluxes saved from hydro solver



$$q^{\text{coarse}} = \tilde{q}^{\text{coarse}} - \Delta t \left( F^{\text{coarse}} - \sum_{j,k} F_{j,k}^{\text{fine}} \right)$$

Uncorrected  
coarse value

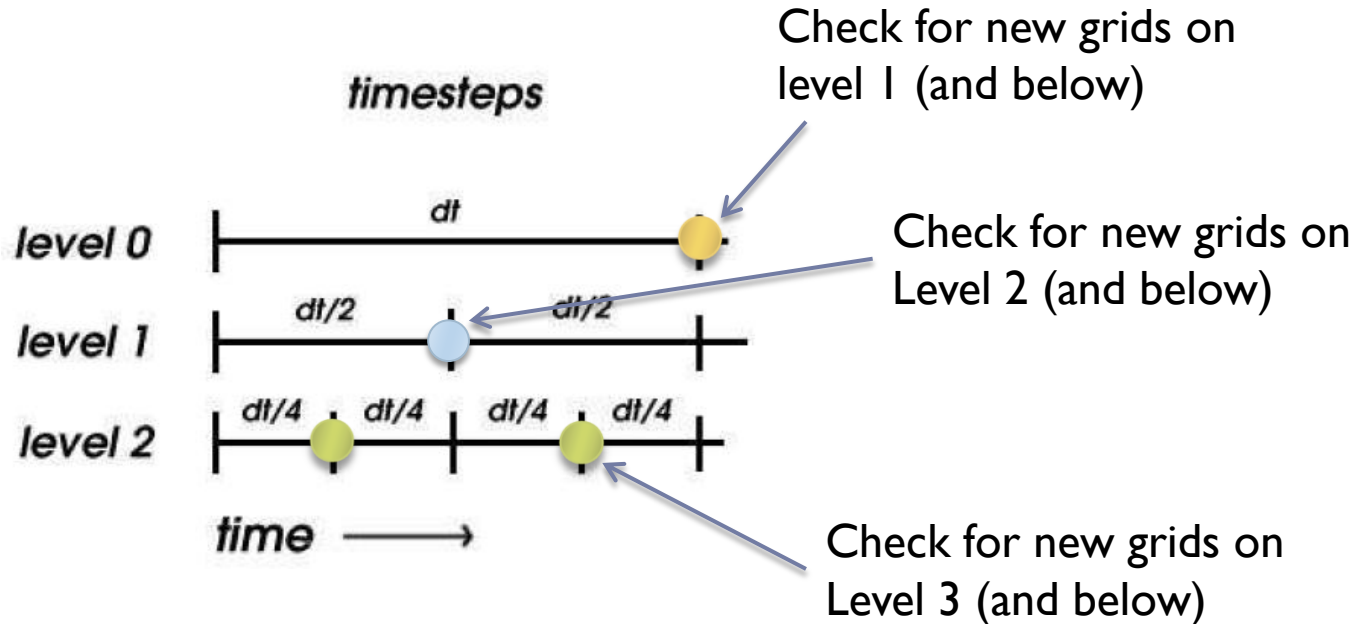
Coarse flux  
across boundary

Sum of fine fluxes  
Over 4 (in 3D)  
abutting fine cells



# Rebuilding the Hierarchy: RebuildHierarchy

- ▶ Need to check for cells needing more refinement



# Refinement Criteria – `grid::SetFlaggingField`

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- ▶ Many ways to flag cells for refinement

- ▶ CellFlaggingMethod =

```
1 - refine by slope
2 - refine by baryon mass
3 - refine by shocks
4 - refine by particle mass
6 - refine by Jeans length
7 - refine if cooling time < cell width/sound speed
11 - refine by resistive length
12 - refine by defined region "MustRefineRegion"
13 - refine by metallicity
```

- ▶ Then rectangular grids must be chosen to cover all flagged cells with minimum “waste”

- ▶ Done with machine vision technique

- ▶ Looks for edges (inflection points in number of flagged cells)

- ▶ ProtoSubgrid class



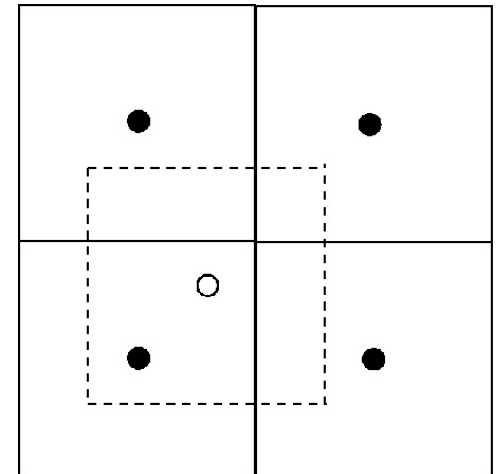


## III. Gravity

# Self-Gravity (SelfGravity = 1)

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- ▶ Solve Poisson equation
- ▶ PrepareDensityField
  - ▶ BaryonField[Density] copied to GravitatingMassField
  - ▶ Particle mass is deposited in 8 nearest cells (CIC)
    - ▶ Particle position advanced by  $\frac{1}{2}$  step
    - ▶ DepositParticleMassField
- ▶ Root grid (level 0):
  - ▶ Potential solved with FFT
$$\tilde{\phi}(k) = G(k)\tilde{\rho}(k).$$
    - ▶ ComputePotentialFieldLevelZero
  - ▶ Potential differenced to get acceleration
    - ▶ grid::ComputeAccelerationField





# Self-Gravity

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## ▶ Subgrids:

- ▶ Potential interpolated to boundary from parent
  - ▶ `Grid::PreparePotentialField`
- ▶ Each subgrid then solves Poisson equation using multigrid
  - ▶ `Grid::SolveForPotential`
- ▶ Note: this has two issues:
  - ▶ Interpolation errors on boundary can propagate to fine levels
    - Generally only an issue for steep potentials (point mass)
    - Ameliorated by having 6 ghost zones for gravity grid
  - ▶ Subgrids can have inconsistent potential gradients across boundary
    - Improved by copying new boundary conditions from siblings and resolving the Poisson equation (`PotentialIterations = 4` by default)
  - ▶ More accurate methods in development



# Other Gravitational sources – grid::ComputeAccelerationFieldExternal

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- ▶ **Can also add fixed potential:**
  - ▶ UniformGravity – constant field
  - ▶ PointSourceGravity – single point source
  - ▶ ExternalGravity – NFW profile





## IV. Particles

# N-body dynamics

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- ▶ Particles contribute mass to `GravitatingMassField`
- ▶ Particles accelerated by `AccelerationField`
  - ▶ Interpolated from grid (from 8 nearest cells)

- ▶ Particles advanced using leapfrog

$$x^{n+1/2} = x^n + (\Delta t/2)v^n$$

$$v^{n+1} = v^n + \Delta t a^{n+1/2}$$

$$x^{n+1} = x^{n+1/2} + (\Delta t/2)v^{n+1}$$

- ▶ `grid::ComputeAccelerations`
  - ▶ Particles stored in the locally most-refined grid
    - ▶ `ParticlePosition`, `ParticleVelocity`, `ParticleMass`
  - ▶ Tracer particles (massless) also available
- 



## IV. Chemistry and Cooling

# Chemistry

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- ▶ Follows multiple species and solve rate equations

$$\frac{\partial \rho_i}{\partial t} + \frac{1}{a} \mathbf{v} \cdot \nabla \rho_i = -\frac{1}{a} \rho_i \nabla \cdot \mathbf{v} + \sum_j \sum_l k_{jl}(T) \rho_j \rho_l + \sum_j I_j \rho_j$$

- ▶ MultiSpecies = 1: H, H<sup>+</sup>, He, He<sup>+</sup>, He<sup>++</sup>, e<sup>-</sup>
- ▶ MultiSpecies = 2: adds H<sub>2</sub>, H<sub>2</sub><sup>+</sup>, H<sup>-</sup>
- ▶ MultiSpecies = 3: adds D, D<sup>+</sup> and HD
- ▶ grid:SolveRateEquations
  - ▶ (or grid::SolveRateAndCoolEquations if RadiativeCooling > 0)
- ▶ Rate equations solved using backwards differencing formula (BDF) with sub-cycles to prevent > 10% changes
  - ▶ Works well as long as chemical timescale not really short



# Radiative Cooling – grid::SolveRadiativeCooling

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- ▶ RadiativeCooling = 1
- ▶ **Two modes:**
  - ▶ MultiSpecies = 0
    - ▶ Equilibrium cooling table (reads file cool\_rates.in)
    - ▶ Sub-cycles so that  $De < 10\%$  in one cooling step
  - ▶ MultiSpecies > 1
    - ▶ Computes cooling rate self-consistently from tracked-species
    - ▶ MetalCooling = 1: adds metal cooling from Glover & Jappsen (2007)
    - ▶ MetalCooling = 2: adds metal cooling from Raymond-Smith code
    - ▶ MetalCooling = 3: Cloudy Cooling table (Smith, Sigurdsson & Abel 2008)
- ▶ RadiationFieldType > 0
  - ▶ Add predefined radiative heating and ionization



# Star Formation

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- ▶ Work in progress – many modes
- ▶ StarParticleCreation > 0
  - ▶ turns on and selects method (1-9)
  - ▶ For more details, see web page
- ▶ StarParticleFeedback > 0
  - ▶ Only valid for methods 1, 2, 7 and 8





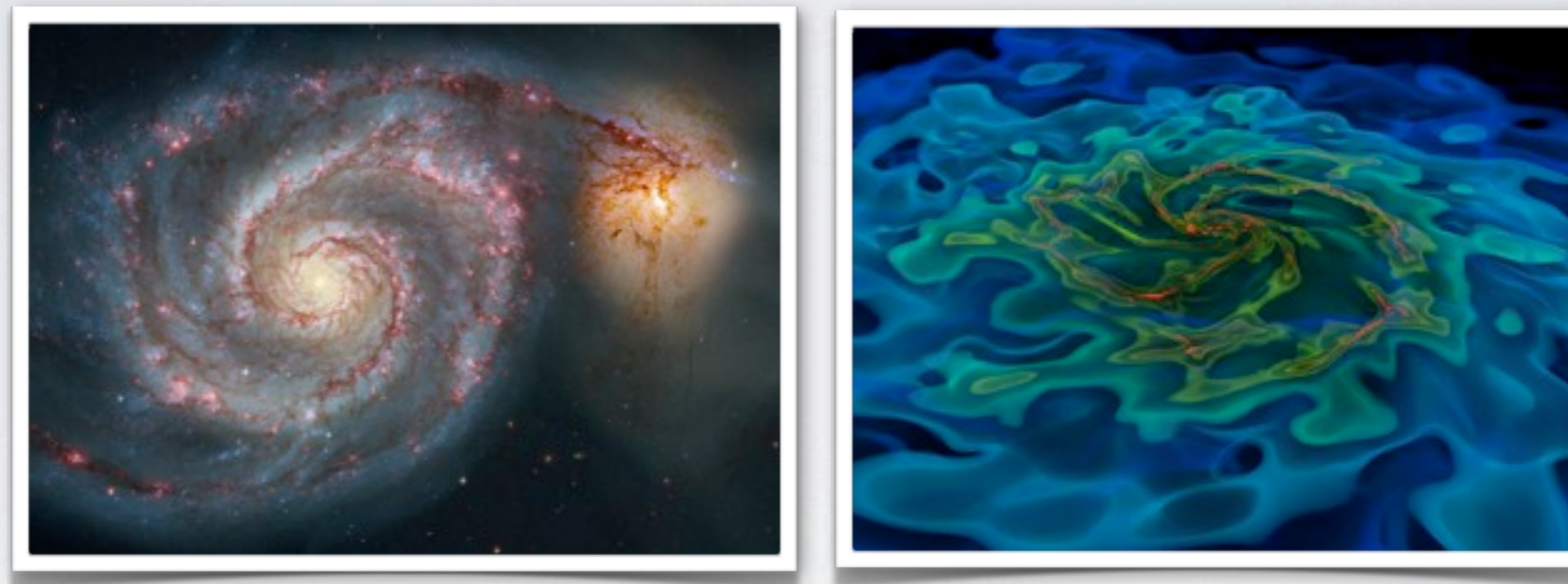
# More Physics in 2.0

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- ▶ See talks tomorrow!



# Galaxy Formation on ENZO with Properly Modeled Stars and MBHs

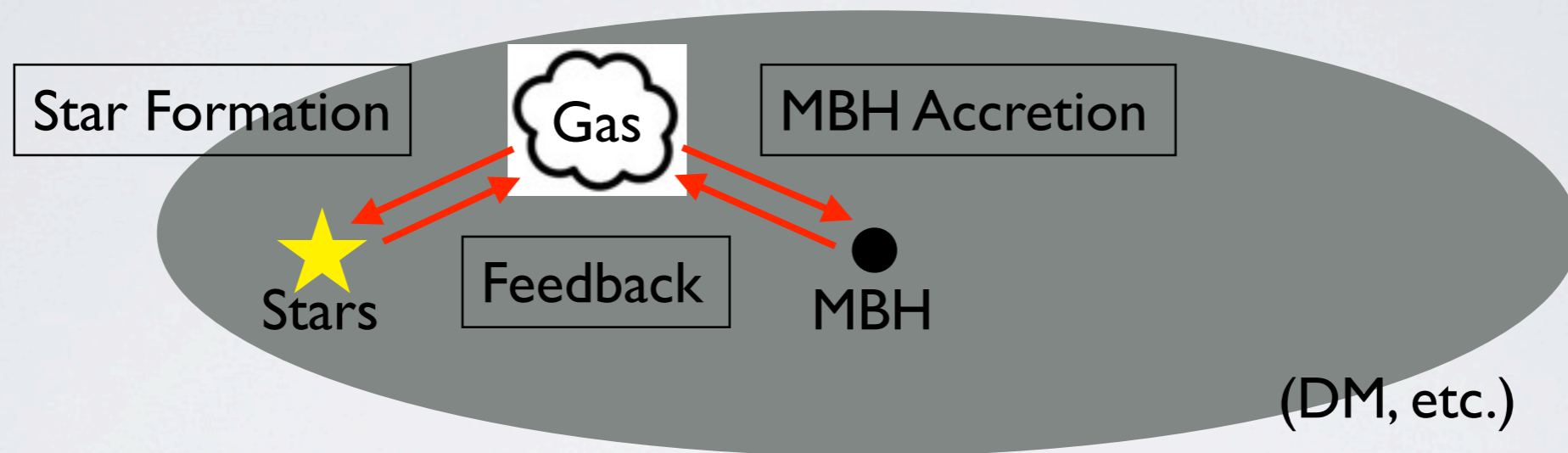


Ji-hoon Kim (KIPAC/Stanford)

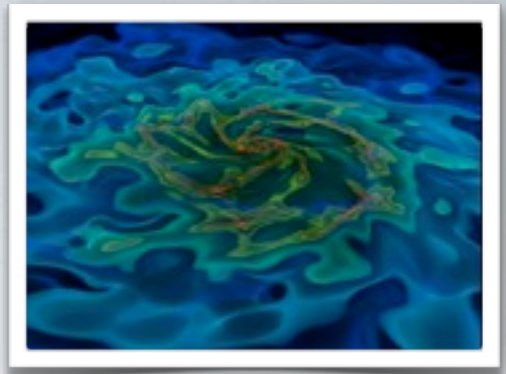
Collaborators: John Wise(Princeton), Marcelo Alvarez(CITA),  
Matthew Turk(UCSD), Tom Abel(Stanford)

# Outline

- Key Components to Understand and Simulate Galaxies



- Modeling the Physics of Galaxy Formation with Stars and MBHs As Best As You Can in **ENZO**
- Simulation Set-ups and Early Results

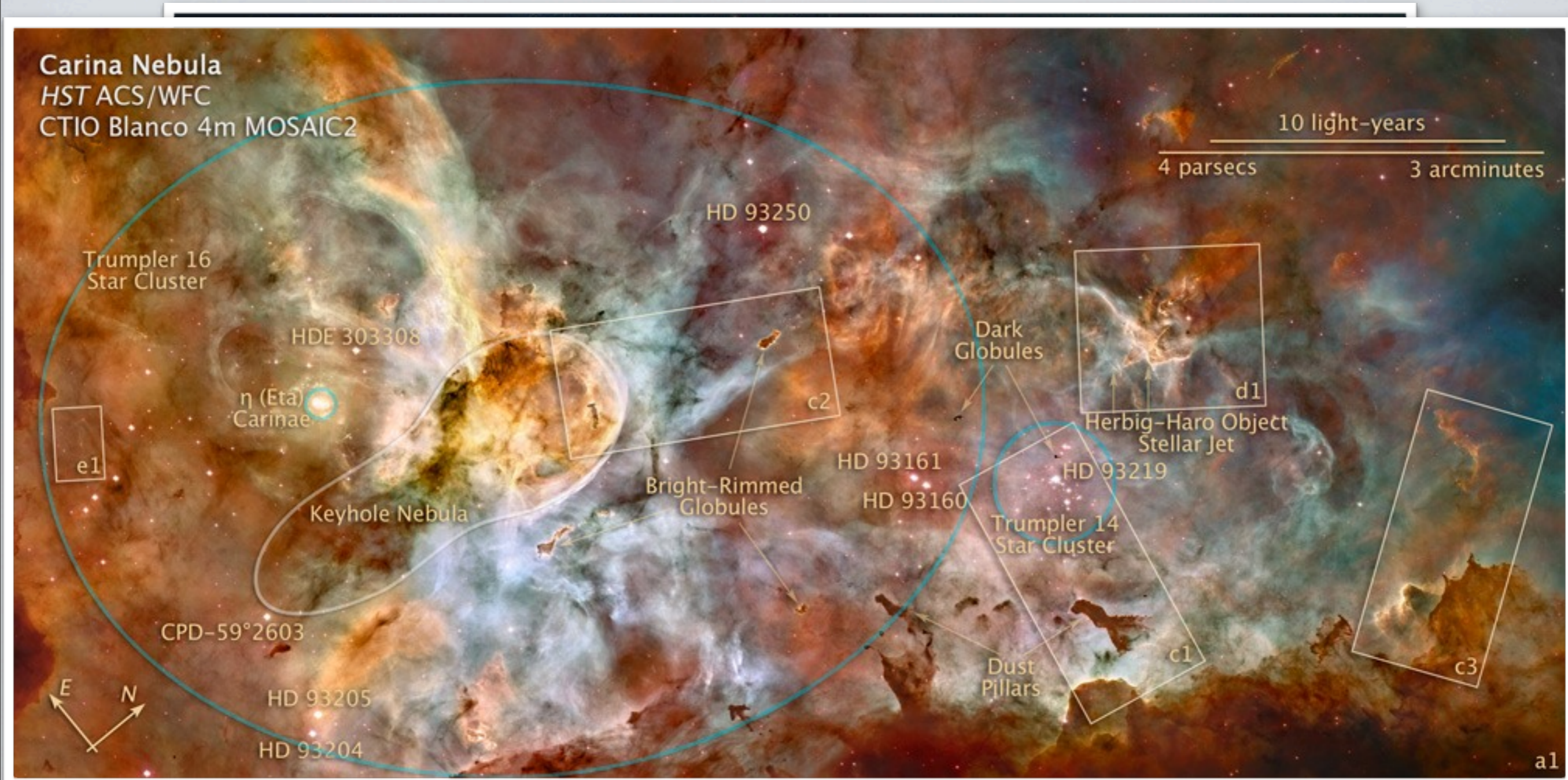


# [Star Formation and Feedback]

# Star Formation = Gas $\rightarrow$ Star

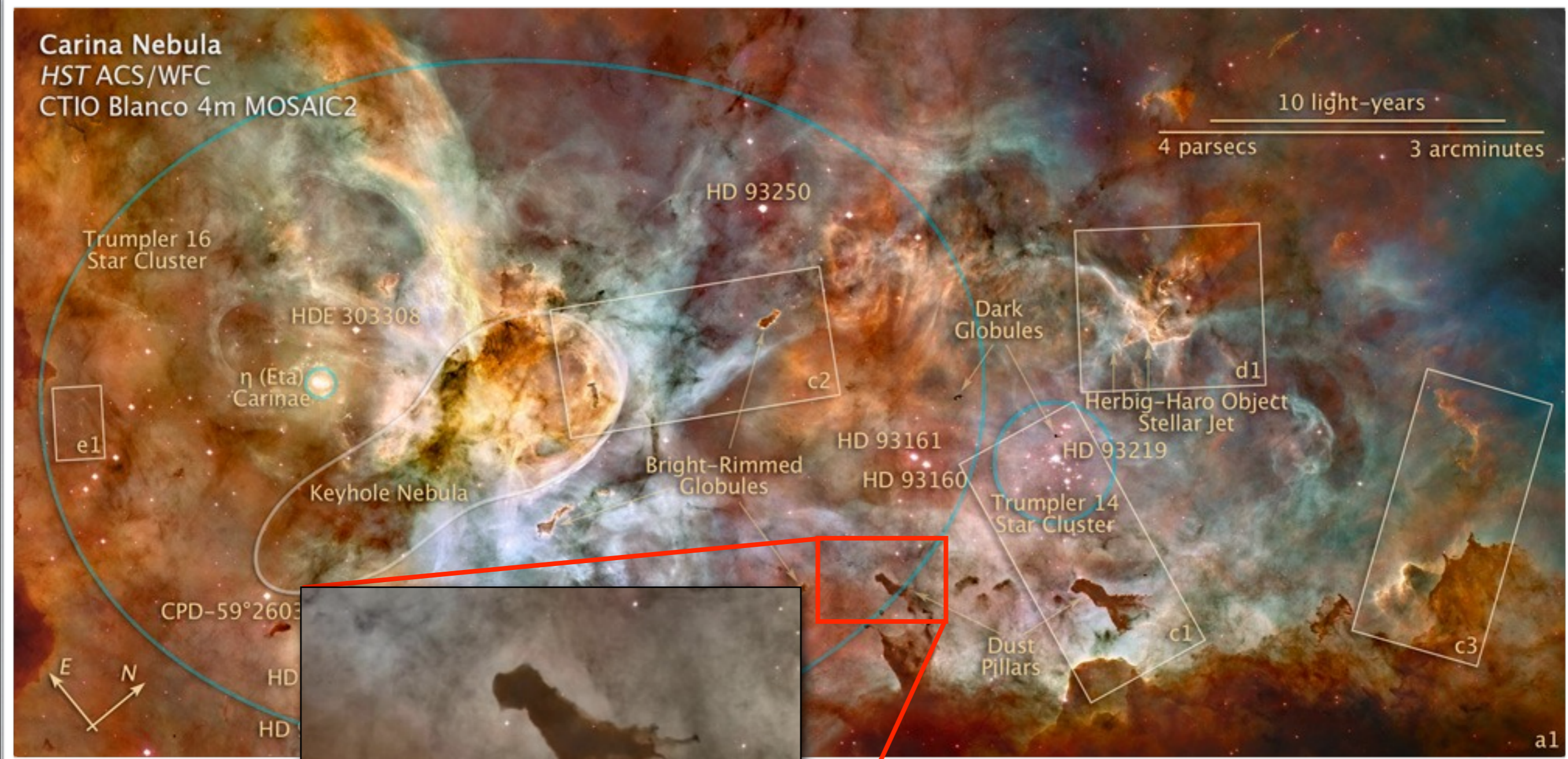


# Star Formation = Gas → Star

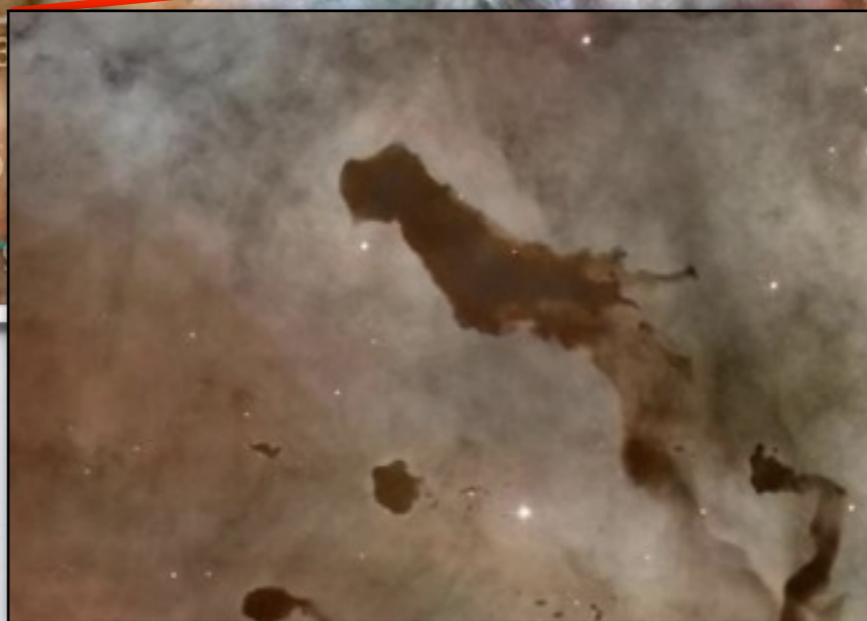
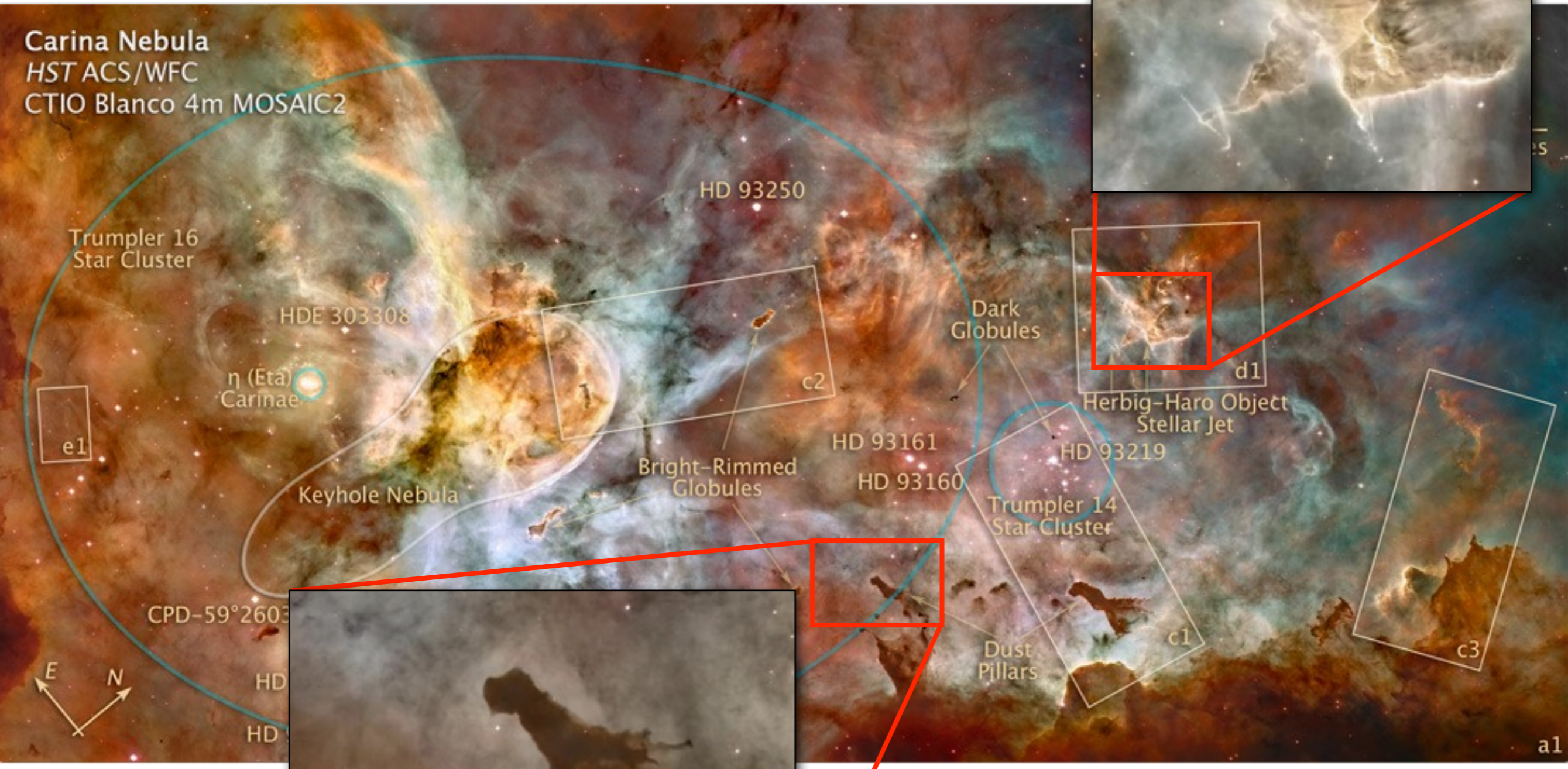


M51 / HST ACS

# Star Formation = Gas → Star

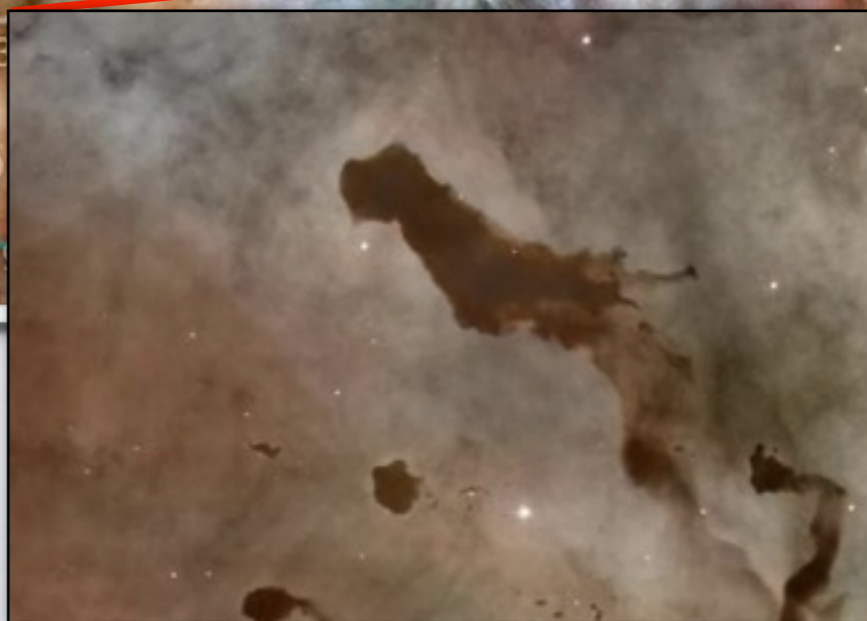
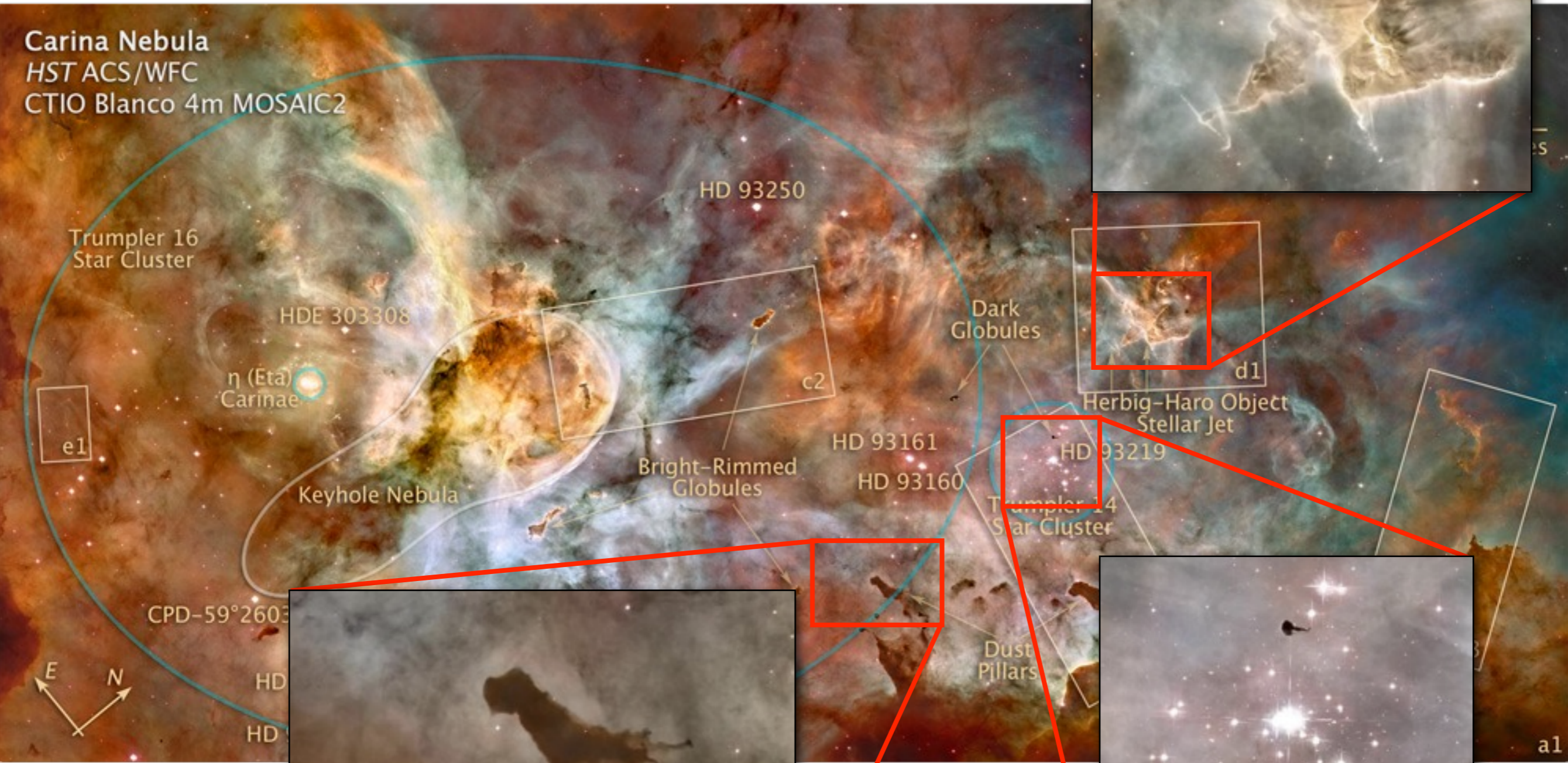


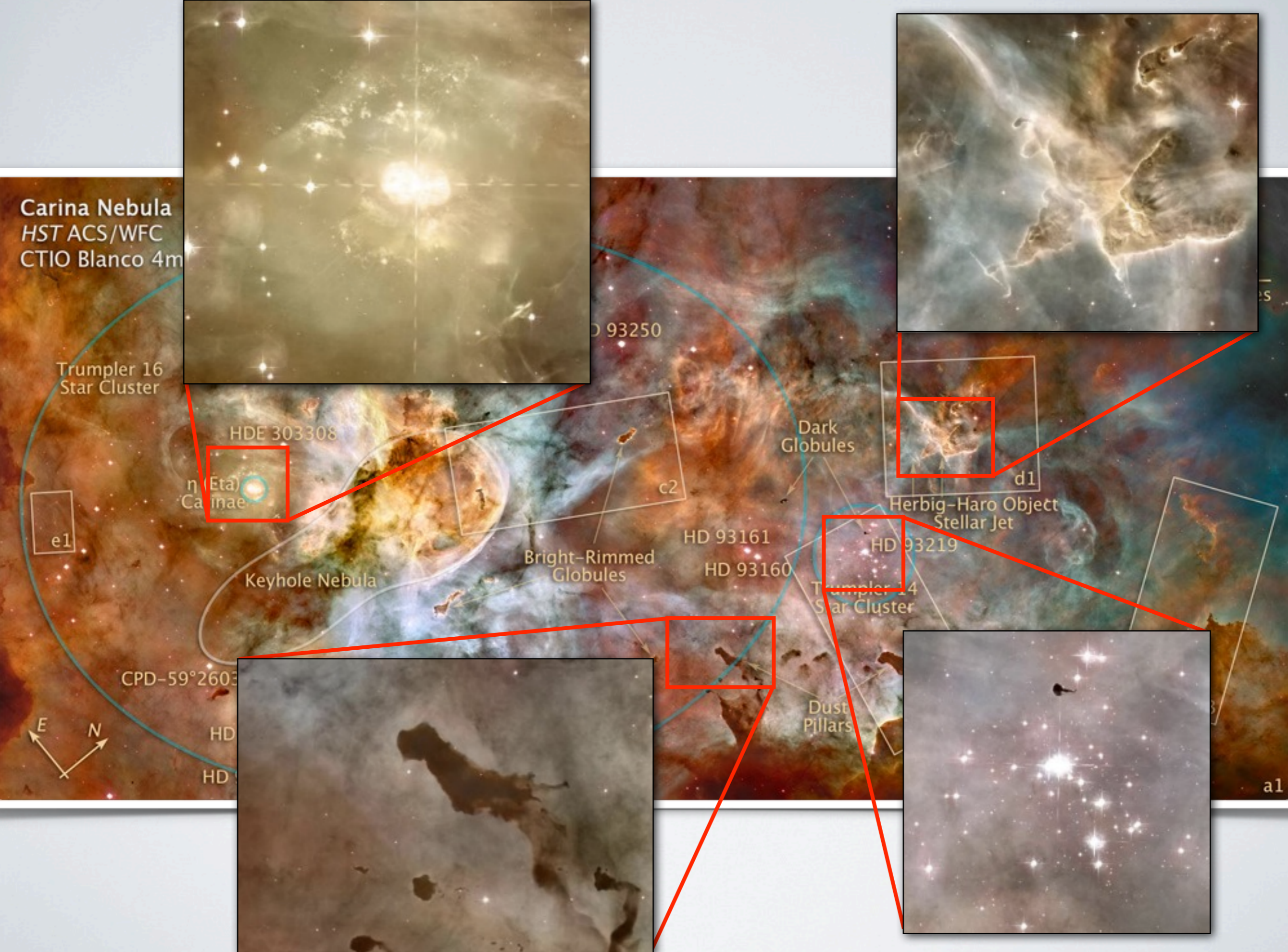
M51 / HST ACS



M51 / HST ACS







Carina Nebula  
HST ACS/WFC  
CTIO Blanco 4m

Trumpler 16  
Star Cluster

HDE 303308

η (Eta)  
Carinae

e1

Keyhole Nebula

Bright-Rimmed  
Globules

c2

Dark  
Globules

d1

Herbig-Haro Object  
Stellar Jet

HD 93161

HD 93160

HD 93219

Trumpler 14  
Star Cluster

CPD-59°2603

HD

HD

Dust  
Pillars

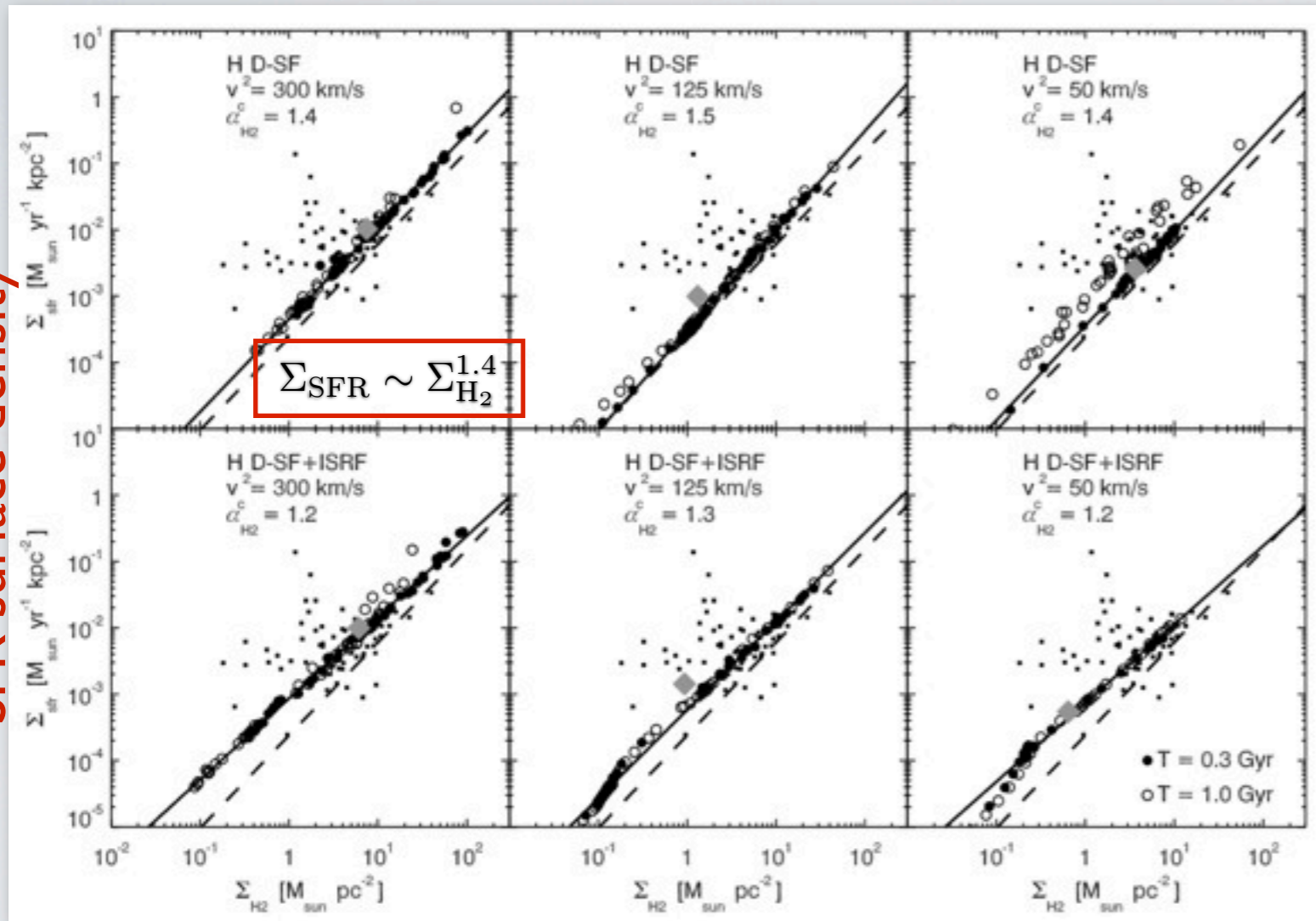
a1



# Previous SF Recipes

(so far in **particle-based** simulations)

SFR surface density →



H<sub>2</sub> surface density →

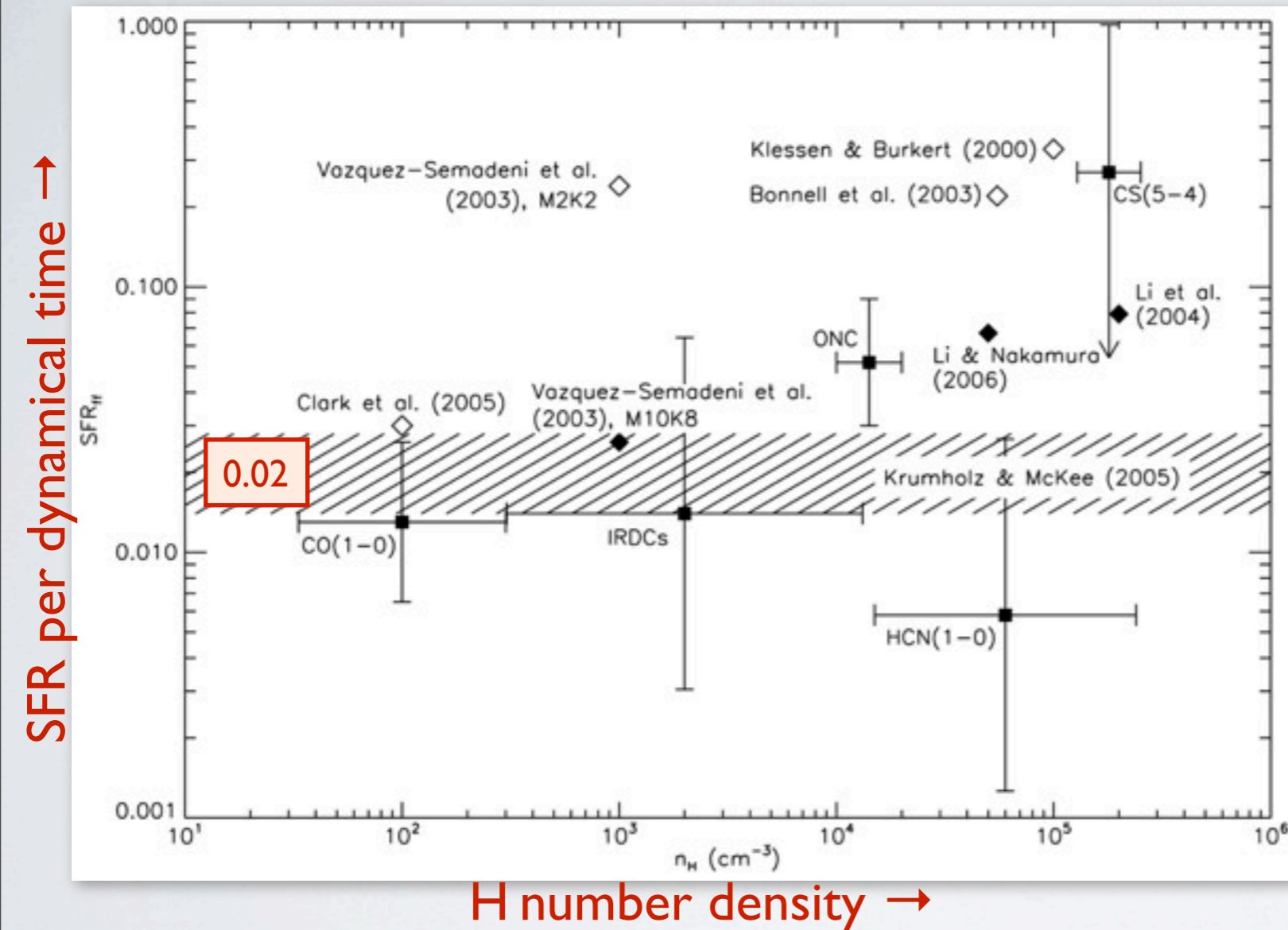
Robertson & Kravtsov (2008),  
Kennicutt-Schmidt relation

- Dominated mostly by the SF recipe using the **Schmidt relation (1959)**

$$\dot{\rho}_* = (1 - \beta) f_{H_2} \frac{\rho_g}{t_*} \left( \frac{n_H}{10 h^2 \text{ cm}^{-3}} \right)^{0.5}$$

- Apply thermal feedback or effective EOS to describe SNe feedback

# Slow SF in Molecular Clouds



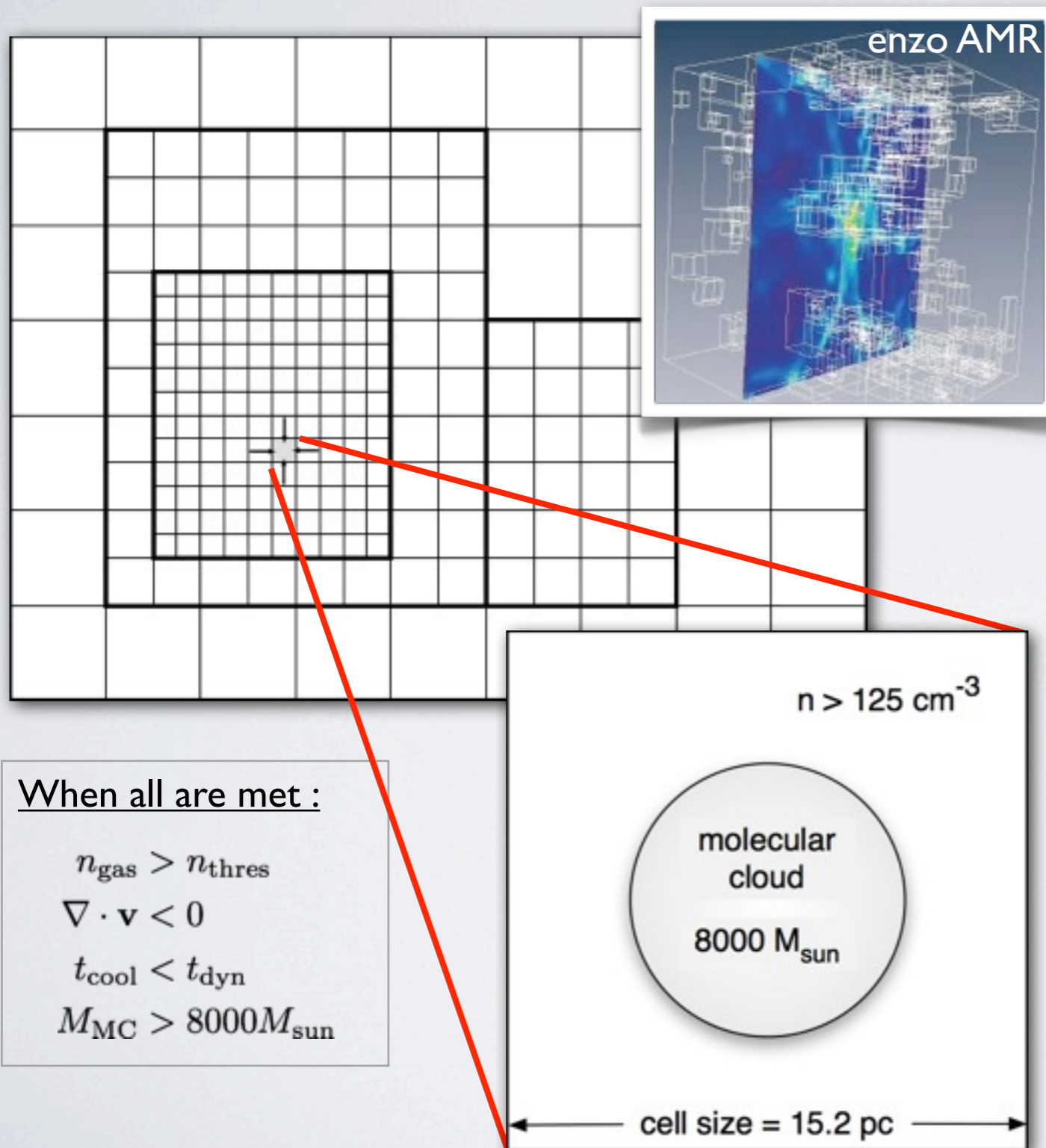
Krumholz & Tan (2007)

- **Very slow** due to turbulence, B-field, protostellar wind, etc.; should be reflected in galaxy-scale studies

$$SFR_{ff} \sim 0.02$$

- MCs ( $10^4$ - $10^5 M_{\text{sun}}$ ) could be the **basic units** that can be represented in galaxy formation sims

# MC Particle - Formation



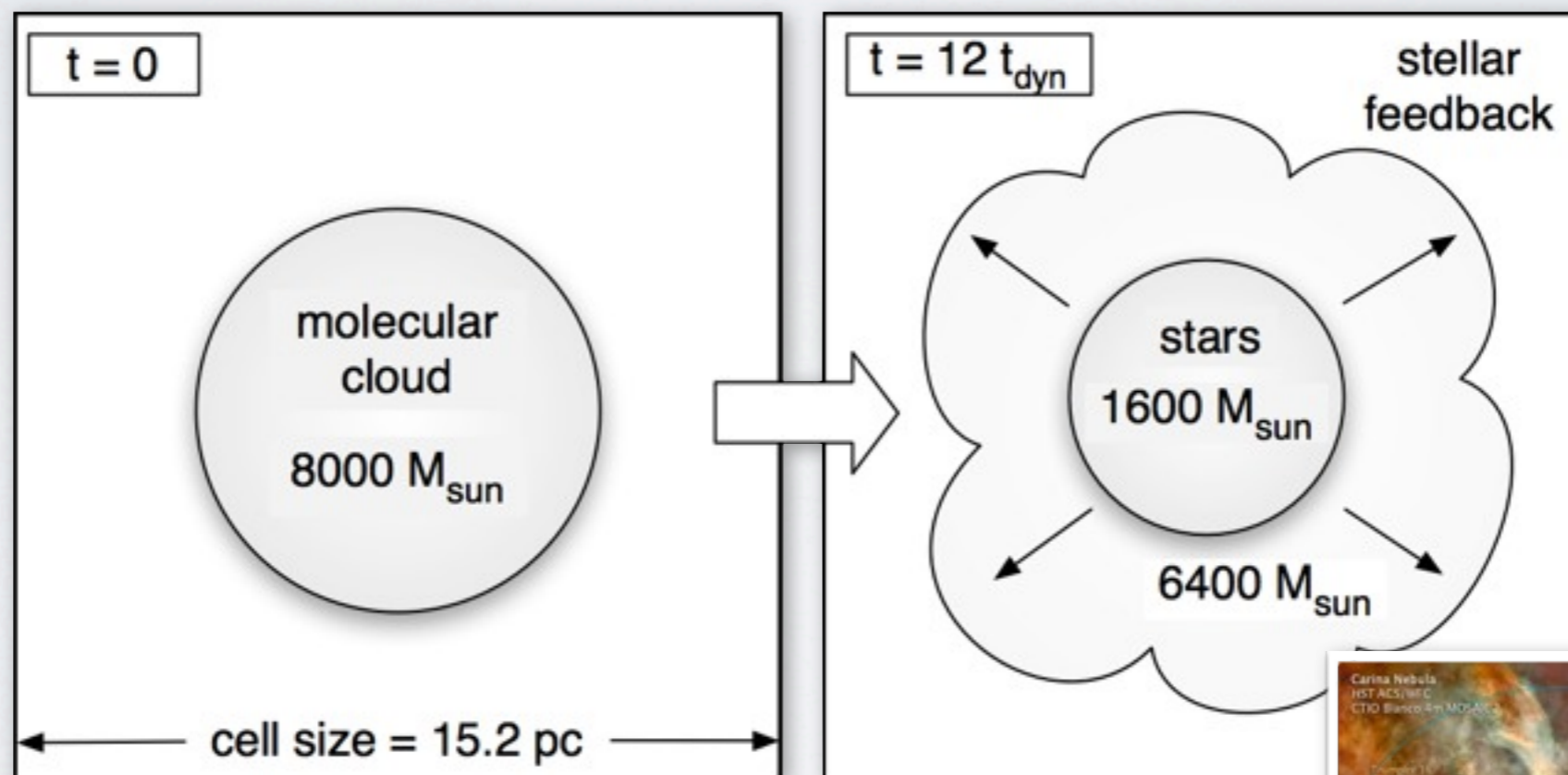
- Max resolution of **15.2 pc**  
=  $L_{\text{Jeans}}$  of a MC of  
125 particles/cm<sup>3</sup> at 960 K

$$M_{\text{MC}} = \epsilon_* \rho_{\text{gas}} \Delta x^3$$

- Self-consistently deposit a particle when a cell of a typical MC size actually becomes **Jeans unstable**
- each particle describes a MC of  $8000 M_{\text{sun}}$

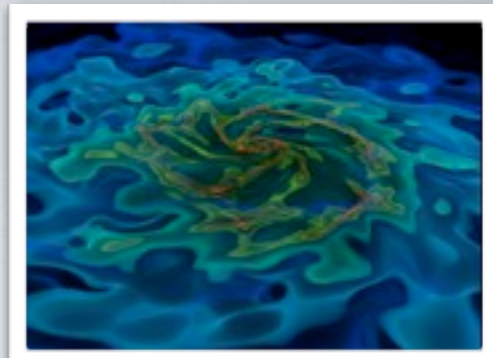
# MC Particle - Feedback

- Both mass and energy are added back to gas
  - **80%** of the MC mass slowly comes back to gas for  $12 t_{\text{dyn}}$
  - carries the **thermal energy** of  $10^{51}$  ergs per  $M_{\text{star}} = 750 M_{\text{sun}}$

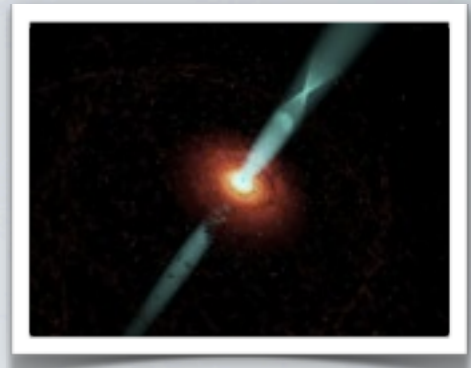


$$M_{\text{star}}(\tau) = 0.2 M_{\text{MC}} \int_0^{\tau} \tau' e^{-\tau'} d\tau'$$





# ~~[Star Formation and Feedback]~~ MC



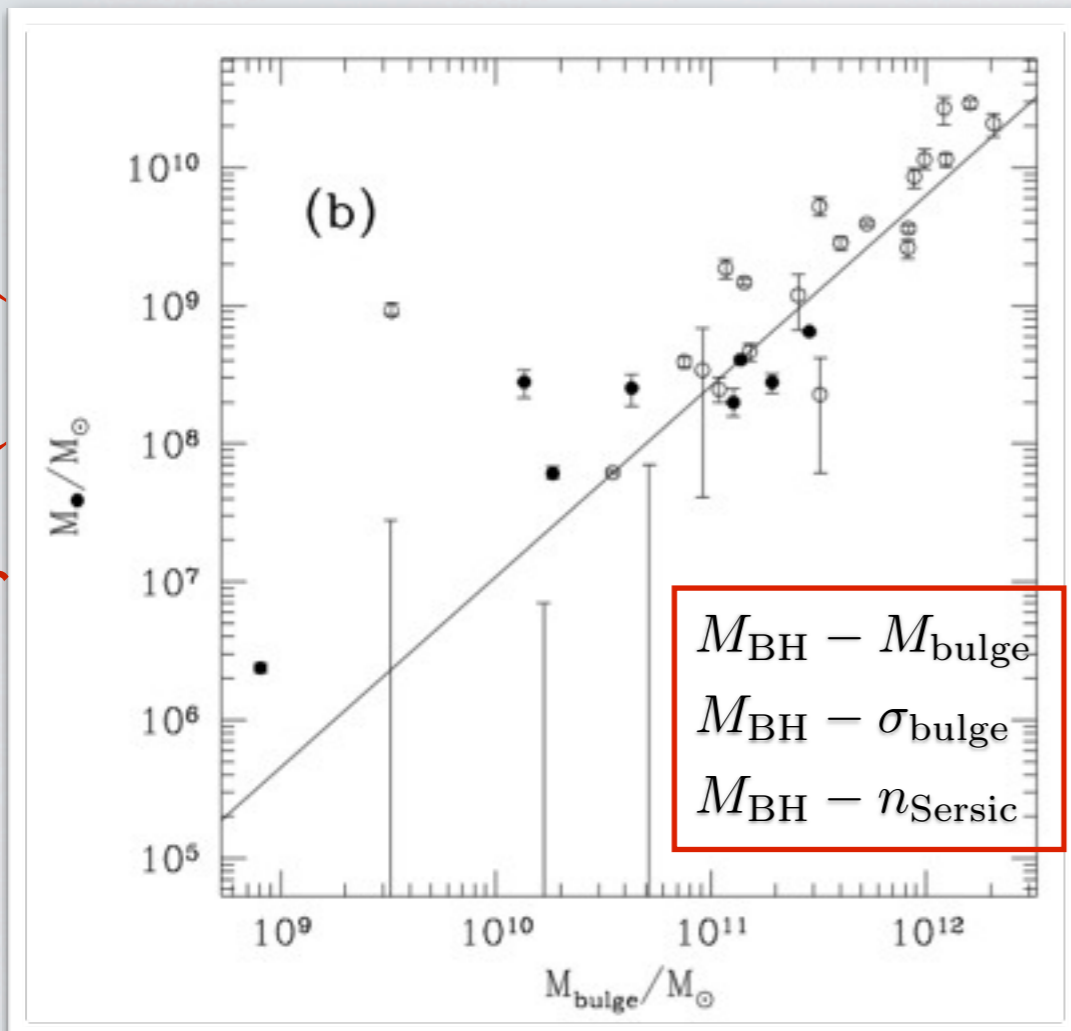
# [MBH Accretion and Feedback]



# Coevolution of Galaxies and MBHs

- Have galaxies and MBHs grown at the same time **under each other's influence?**

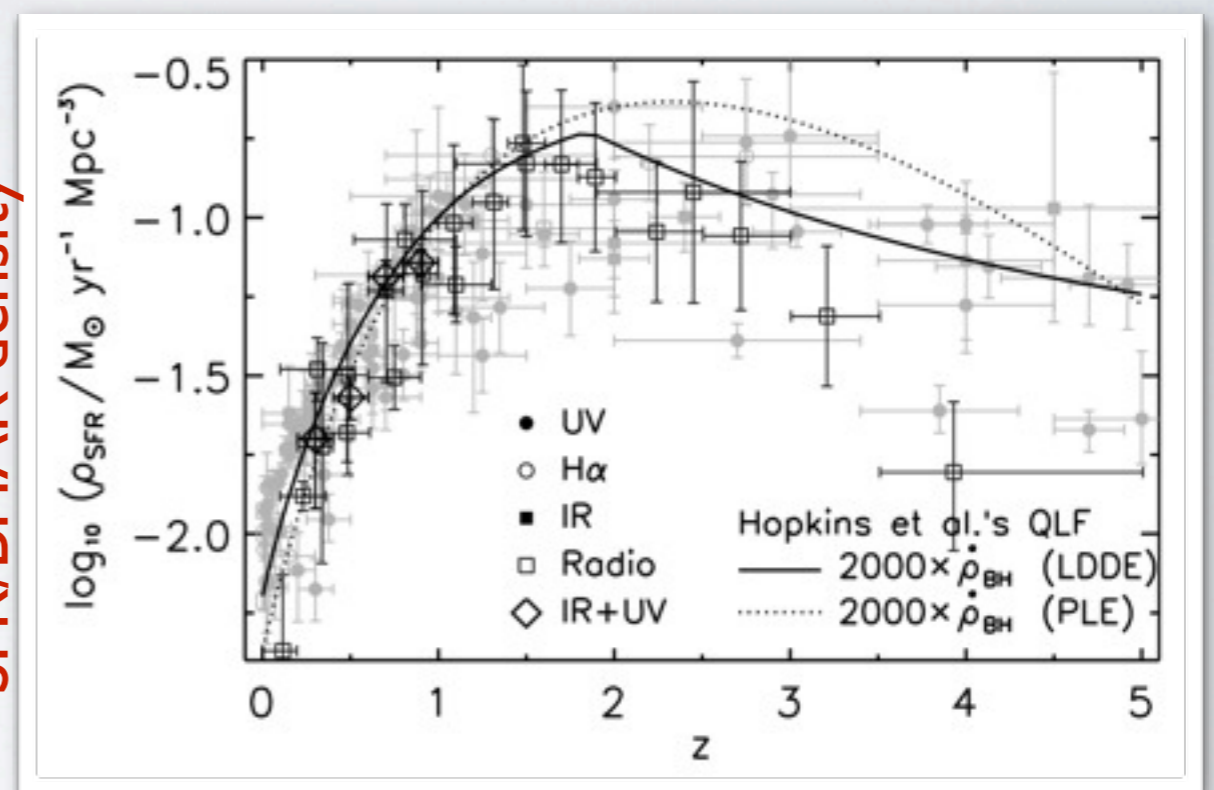
massive dark object (MDO) mass →



bulge mass →

Magorrian et al. (1998)

SFR/BHAR density →



redshift →

Zheng et al. (2009)

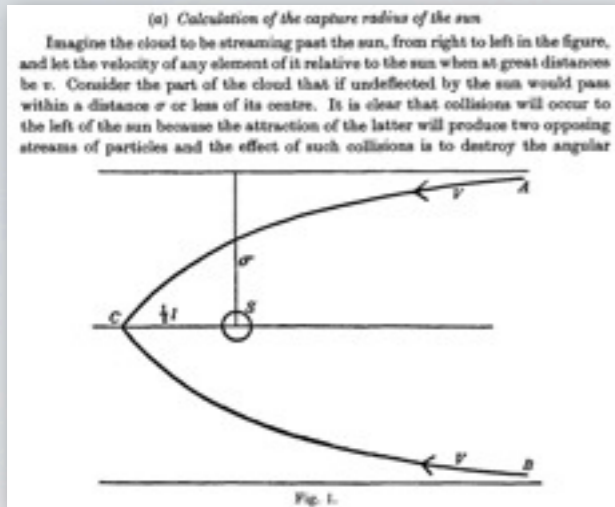
\* Unified model: Silk & Rees (1998), Kauffmann & Haehnelt (2000), etc.

# Second Component!

- GOAL: Study the coevolution of galaxies and MBHs in one comprehensive **self-consistent** framework!

# Previous Sink Particle Recipe

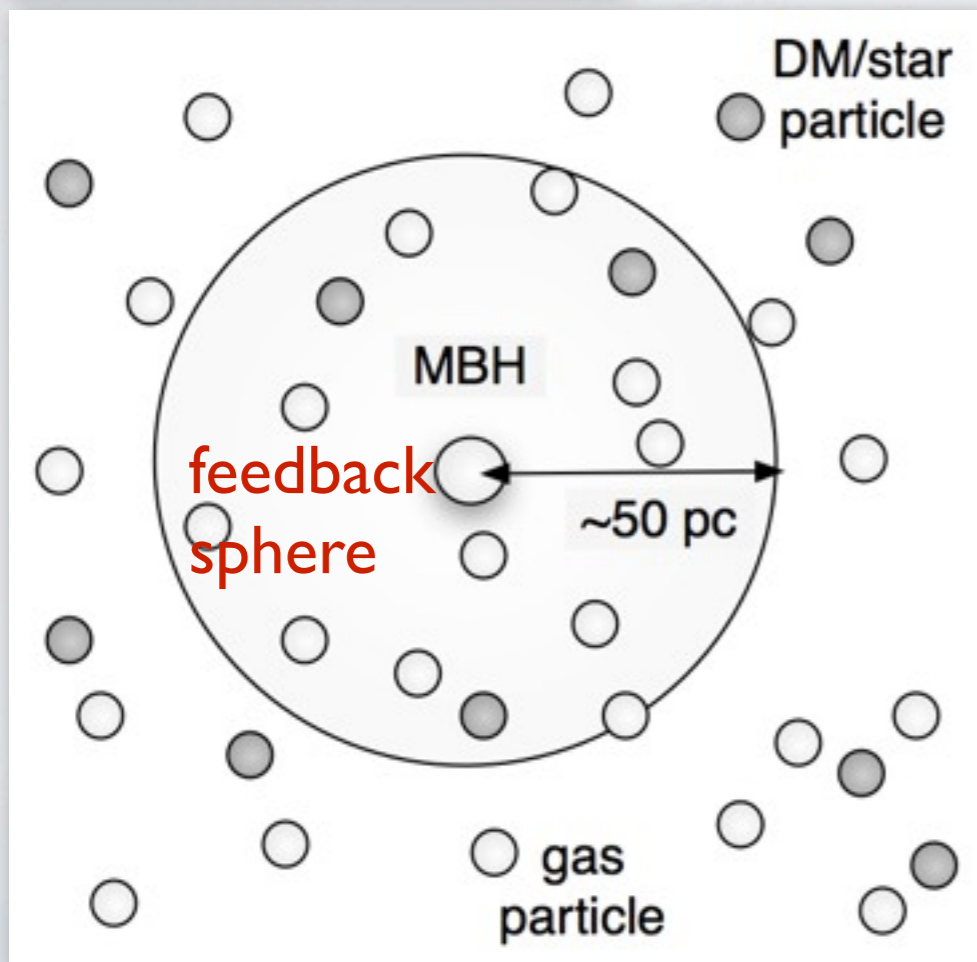
(so far **in particle-based** galaxy formation)



Hoyle & Lyttleton  
(1939)

- Growing MBH based on the spherical **Bondi-Hoyle** accretion argument

$$\dot{M}_{\text{BH}} = \min \left( \frac{4\pi\alpha G^2 M_{\text{BH}}^2 \rho_{\text{B}}}{c_{\text{s}}^3}, \frac{4\pi G M_{\text{BH}} m_{\text{p}}}{\epsilon_{\text{r}} \sigma_{\text{T}} c} \right)$$

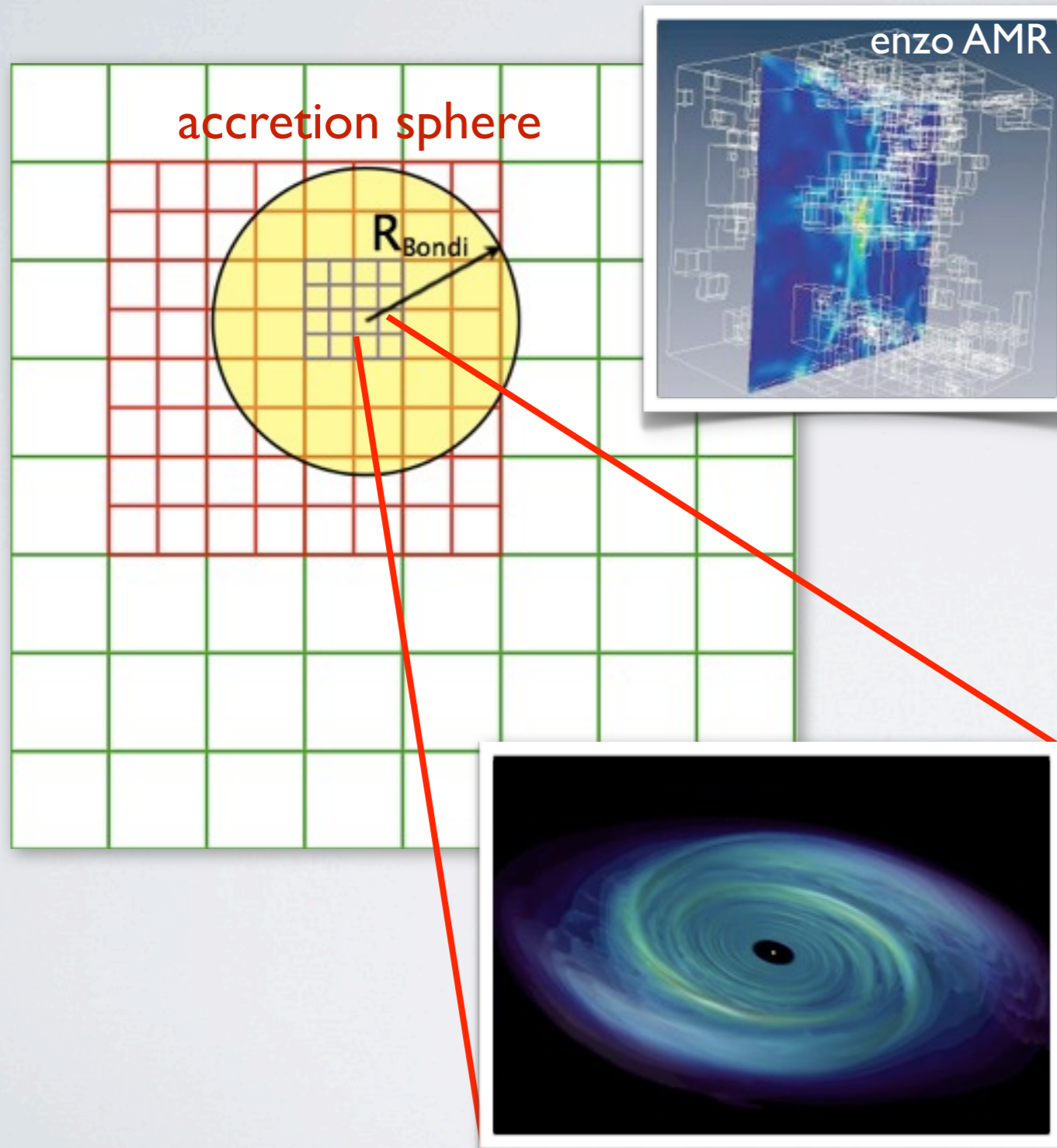


- Kernel-weighted **thermal feedback** (5% most cases) based on accretion rate

$$\dot{E}_{\text{BH,th}} = \epsilon_{\text{f}} \epsilon_{\text{r}} \dot{M}_{\text{BH}} c^2$$

Springel et al. (2005)  
& many others

# MBH Particle - Accretion



- Eddington-limited Bondi estimate with **no tweaks**; subtraction from a sphere of radius  $R_{\text{Bondi}}$

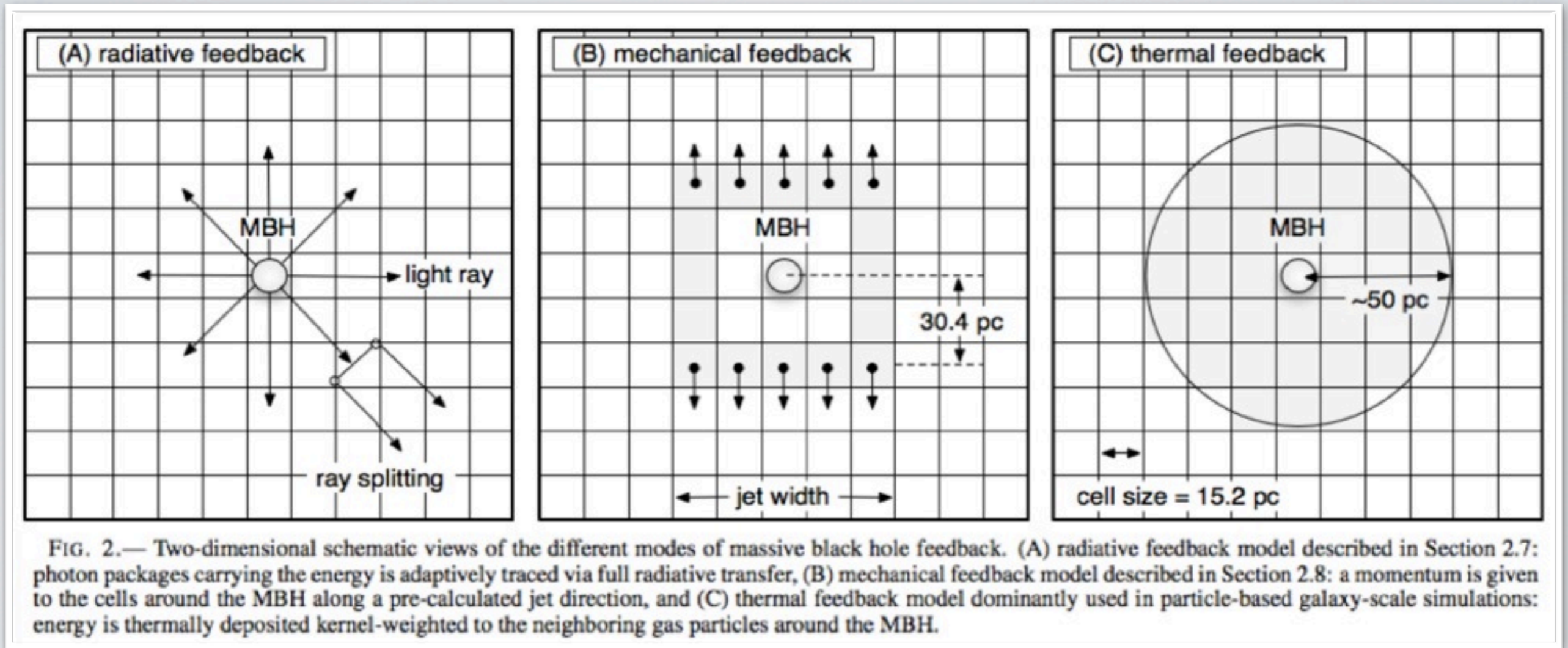
$$\dot{M}_{\text{BH}} = \min \left( \frac{4\pi G^2 M_{\text{BH}}^2 \rho_{\text{B}}}{c_s^3}, \frac{4\pi G M_{\text{BH}} m_{\text{p}}}{\epsilon_r \sigma_{\text{TC}}} \right)$$

- Getting close to **resolving**  $R_{\text{Bondi}}$  of MBHs in galaxy-scale simulations

$$R_{\text{Bondi}} = \frac{2GM_{\text{BH}}}{c_s^2} \simeq 8.6 \text{ pc} \left( \frac{M_{\text{BH}}}{10^5 M_{\odot}} \right) \left( \frac{10 \text{ km/s}}{c_s} \right)^2$$

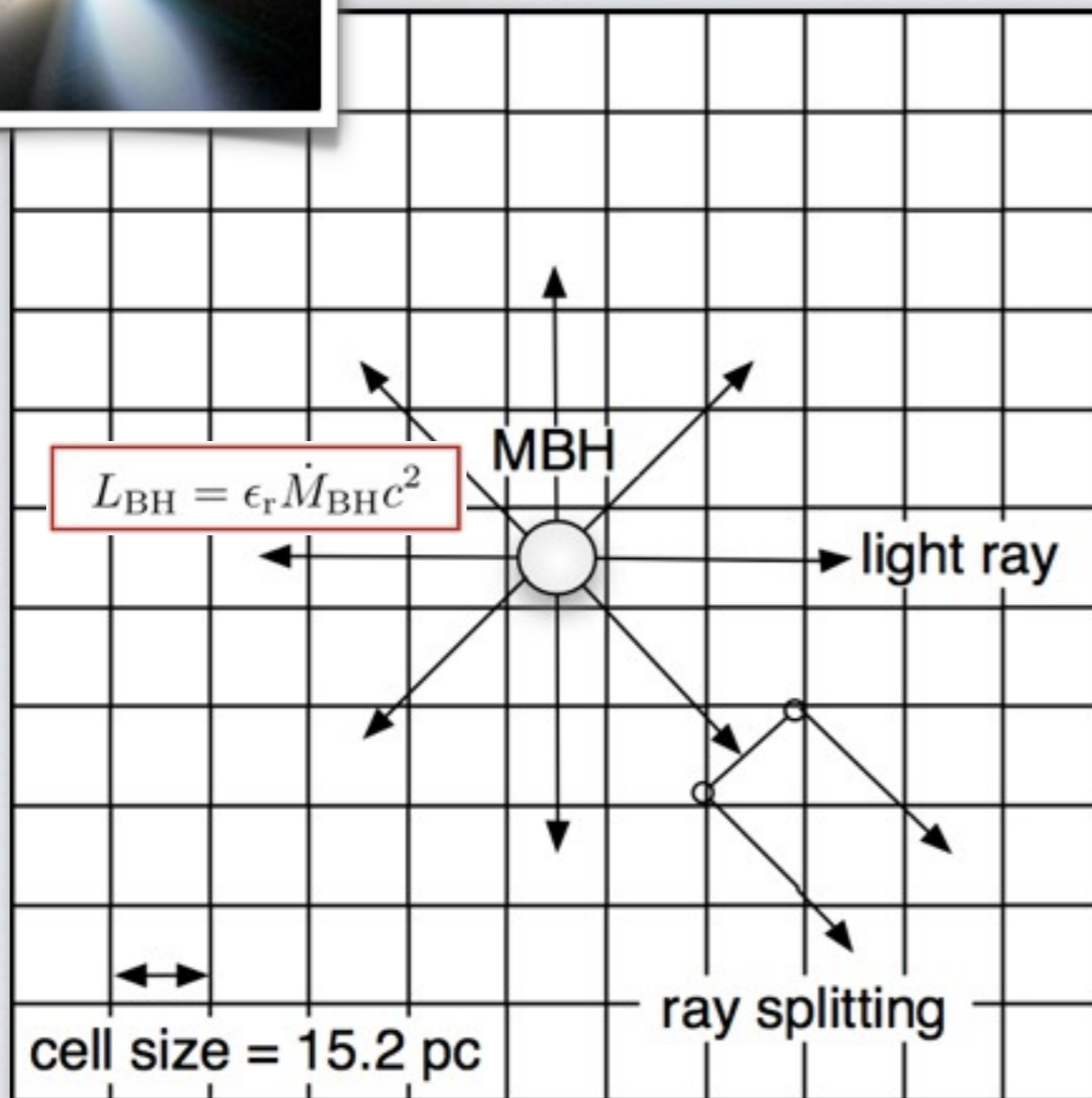
# MBH Particle - Feedback

- Designed **three** different feedback channels; **two** currently in use

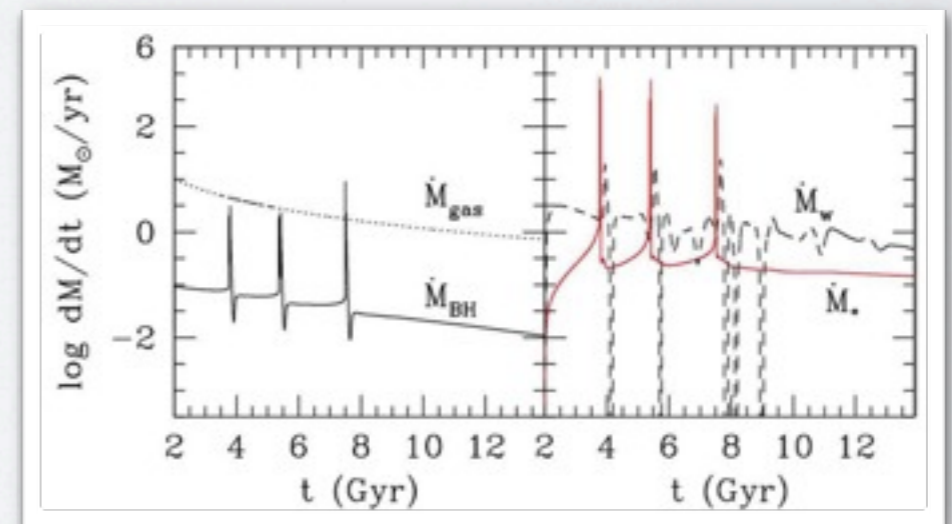


- Kim, Wise, Alvarez, & Abel (2010) in prep.

# (I) MBH Radiative Feedback

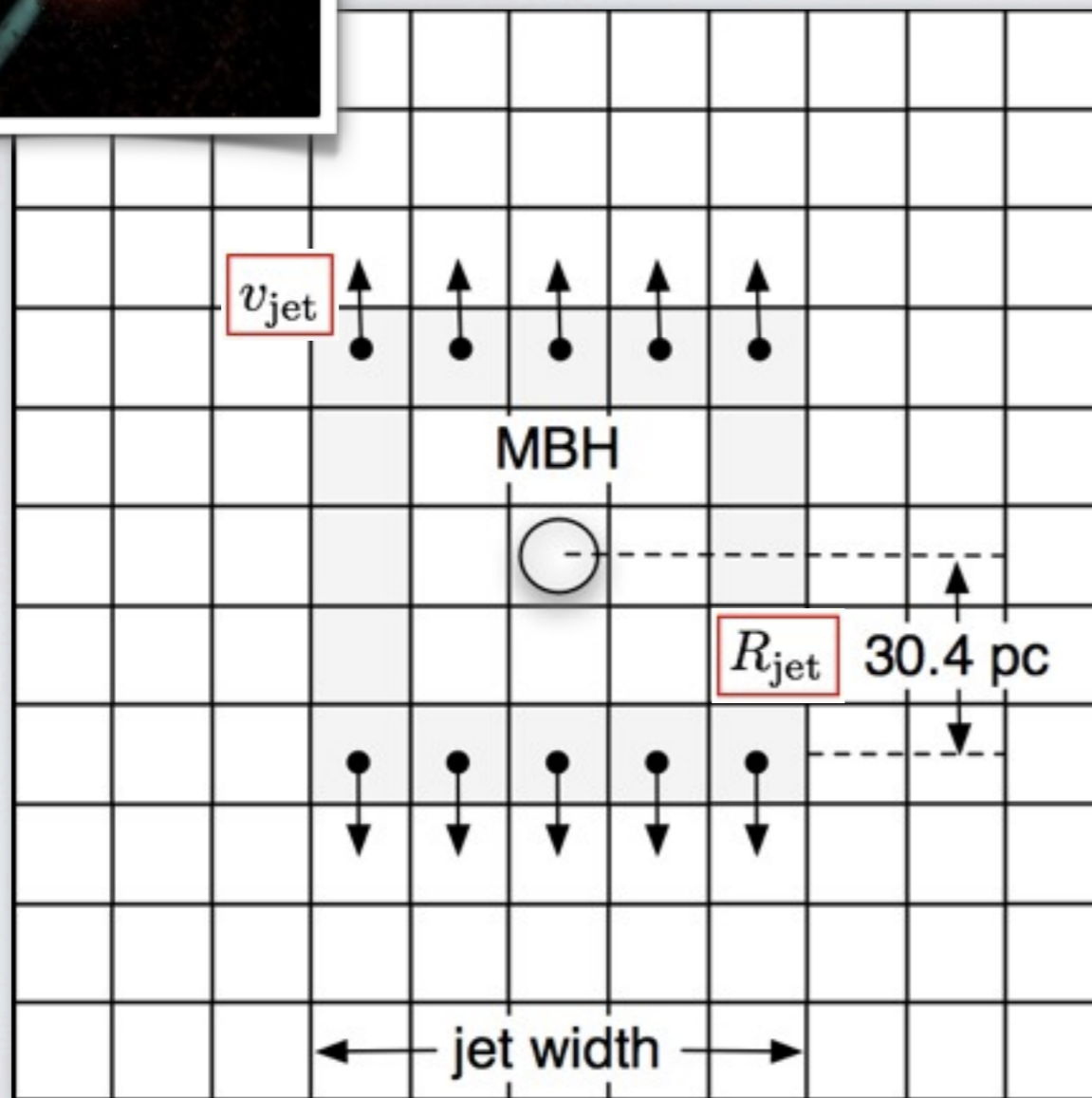
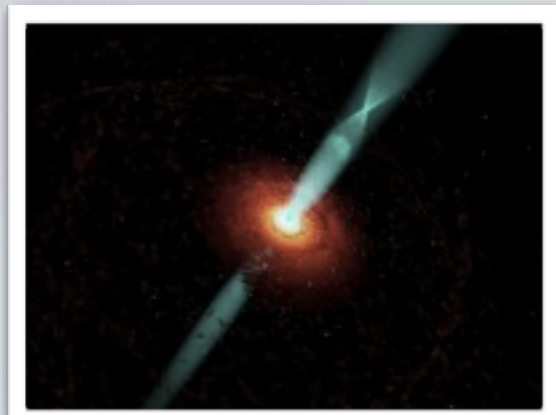


- Full 3D radiative transfer:  
monochromatic **2 keV**  
X-ray photon packages do
  - photoionization (H, He, He<sup>+</sup>)
  - photoheating
  - Compton heating (e<sup>-</sup>)
  - radiation pressure



Ciotti et al. (2010): 1D-model

# (2) MBH Mechanical Feedback



- Mechanical Energy  
= **Potential** Energy  
(jets introduced at  $R_{\text{jet}}$ )  
+ **Kinetic** Energy  
(jets launched with  $v_{\text{jet}}$ )

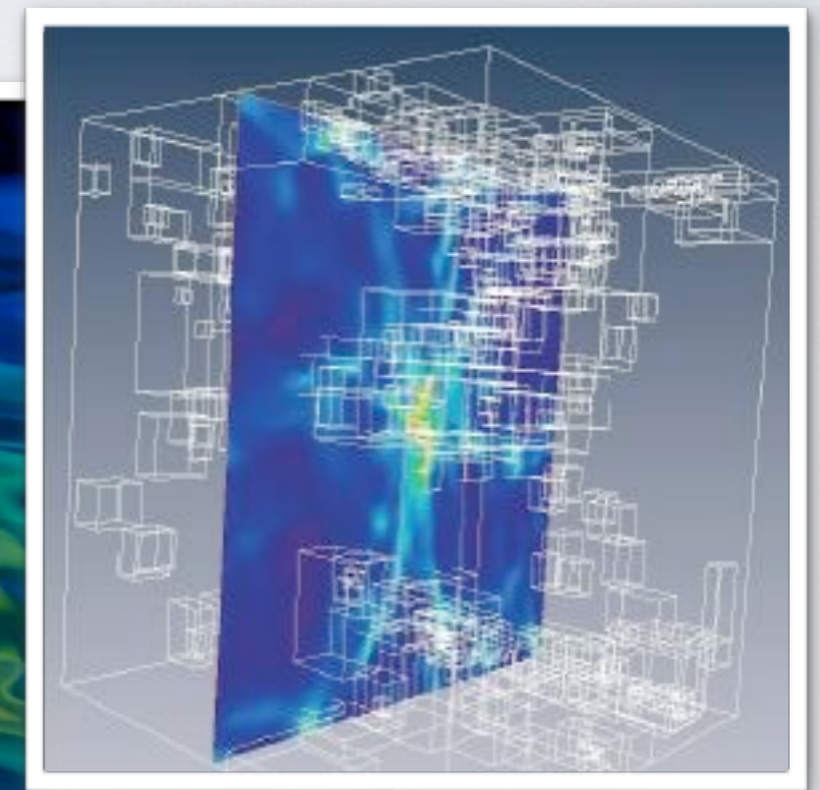
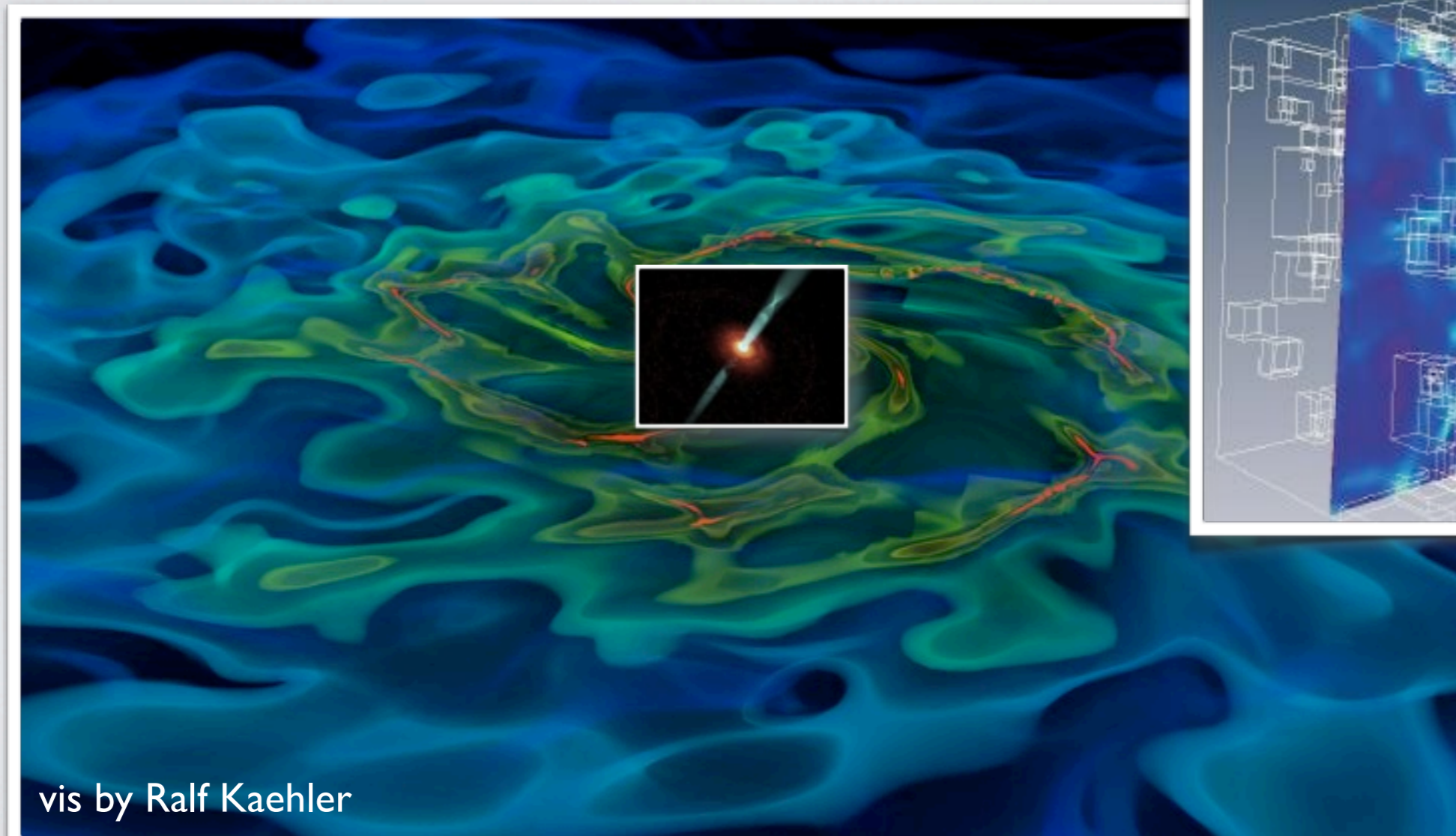
$$\epsilon_{\text{kin}} \equiv \frac{P_{\text{kin}}}{L_{\text{BH}}} = 10^{-4} \quad \text{and} \quad \eta_{\text{jet}} \equiv \frac{\dot{M}_{\text{jet}}}{\dot{M}_{\text{BH}}} = 0.05$$

$$\rightarrow v_{\text{jet}} = c \left( \frac{2\epsilon_{\text{kin}}\epsilon_r}{\eta_{\text{jet}}} \right)^{1/2}$$

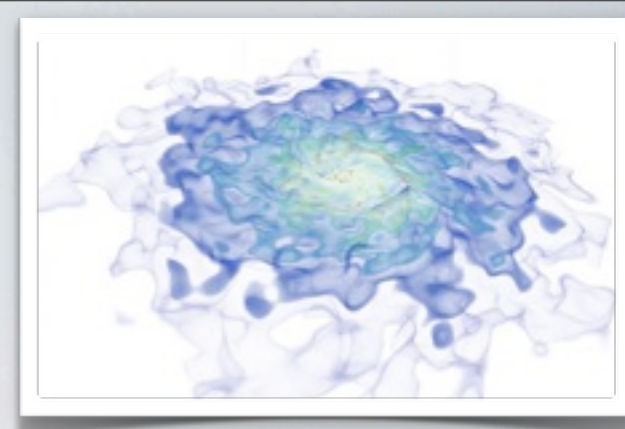
- Directed along  $\vec{L}_{\text{gas-accreted}}$ ;  
injected at every  $300 M_{\text{sun}}$

# Multi-scale Physics

- Resolving things from  $R_{\text{Bondi}}$  to  $R_{\text{galaxy}}$ , from  $10^2$  K to  $10^7$  K  
→ AMR **enzo-2.0** poised to do a better job than ever







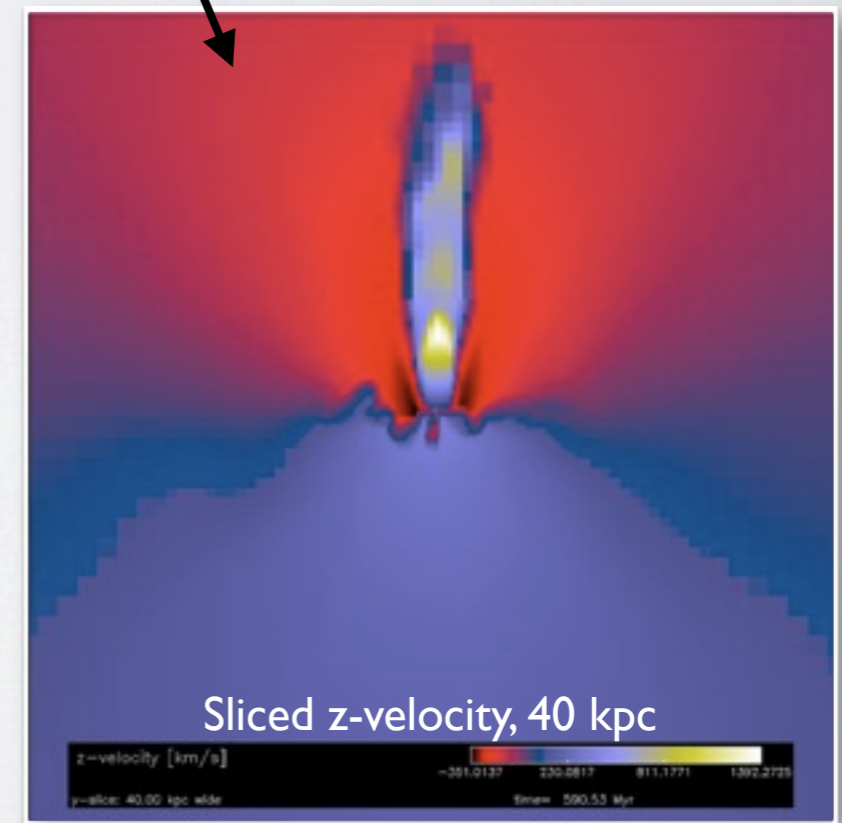
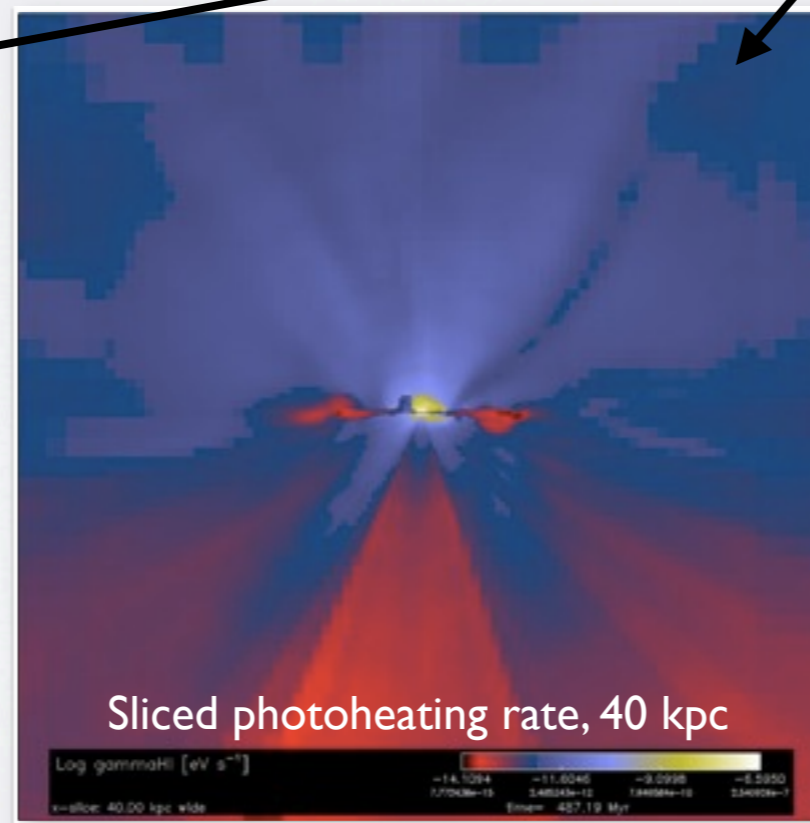
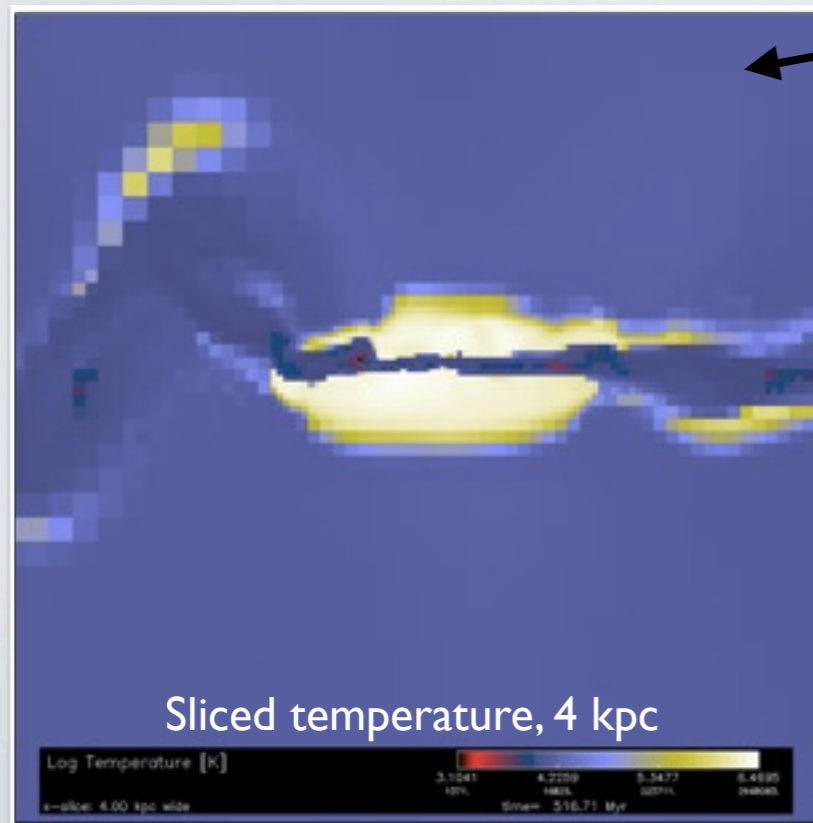
# [Setting Up An Experiment & Early Results]

# Simulation Suite

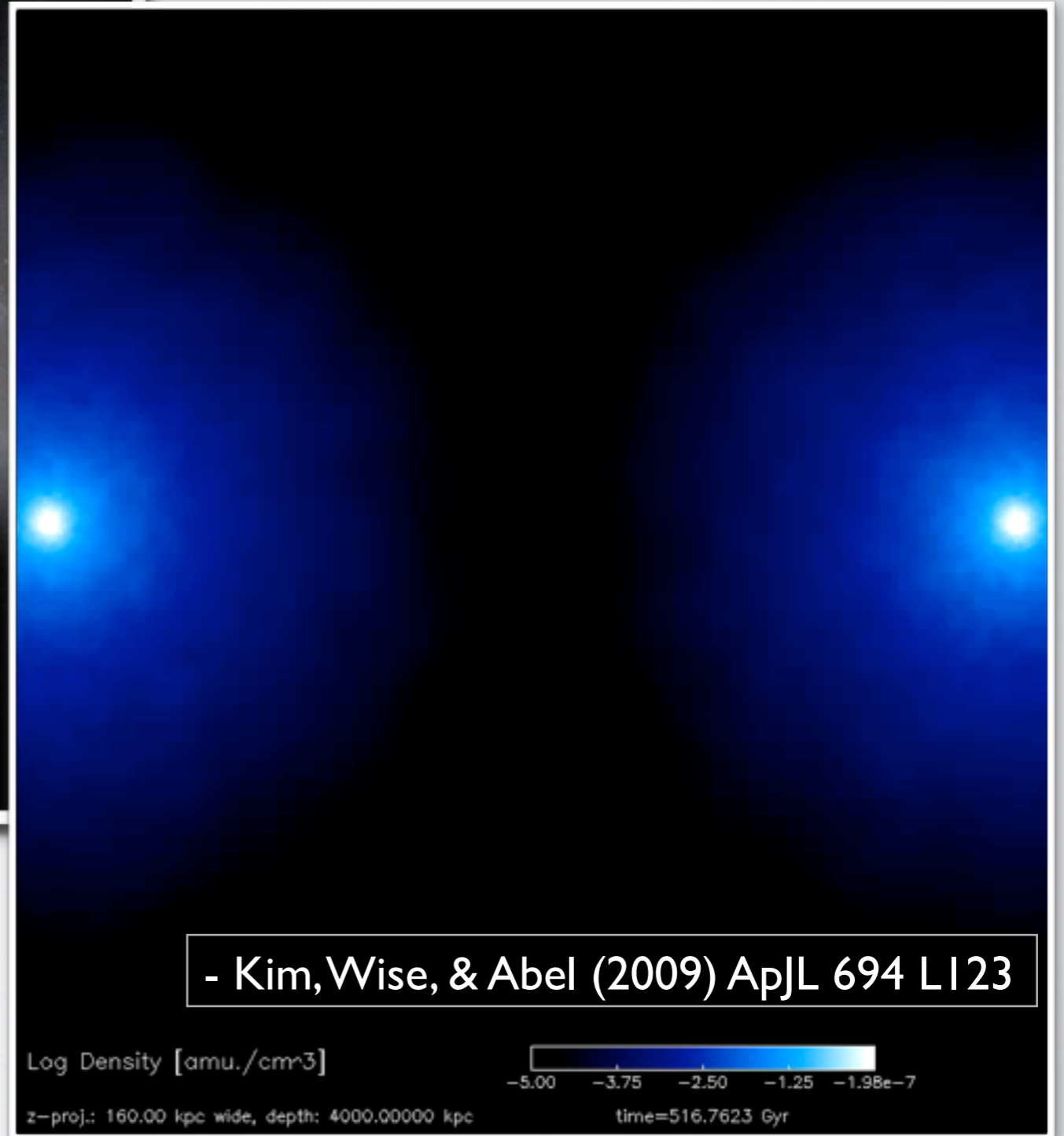
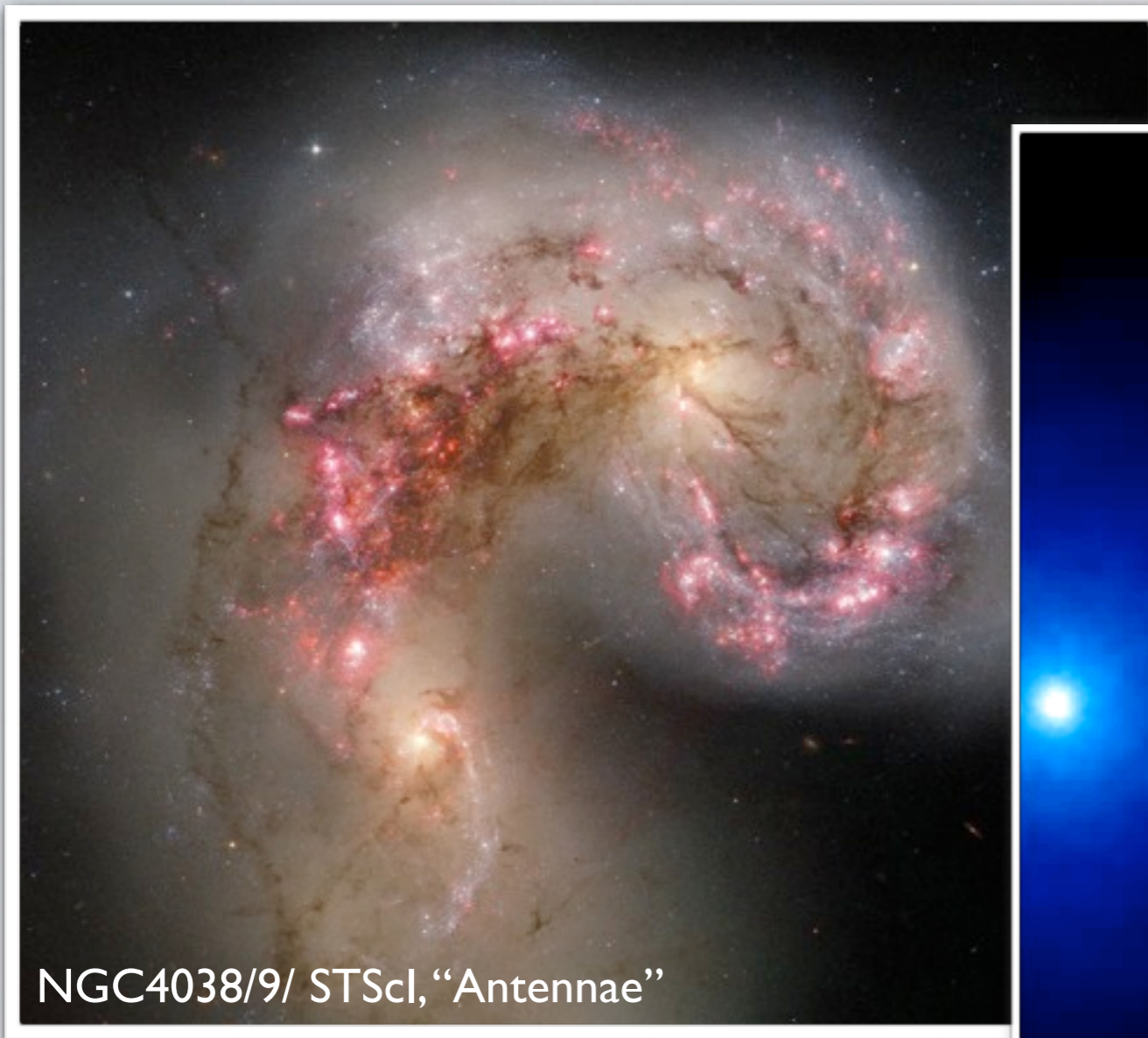
- Ensembles of simulations with **different modes of feedback** to study the galaxy evolution regulated by stellar and MBH feedback

TABLE 1  
SIMULATION SUITE DESCRIPTION

Physics <sup>a</sup>		Sim-NF	Sim-SF	Sim-RF	Sim-MF	Sim-RMF
Molecular cloud formation	(Section 2.4)	○	○	○	○	○
Stellar feedback	(Section 2.5)	×	○	○	○	○
Massive black hole accretion	(Section 2.6)	○	○	○	○	○
Massive black hole radiative feedback	(Section 2.7)	×	×	○	×	○
Massive black hole mechanical feedback	(Section 2.8)	×	×	×	○	○

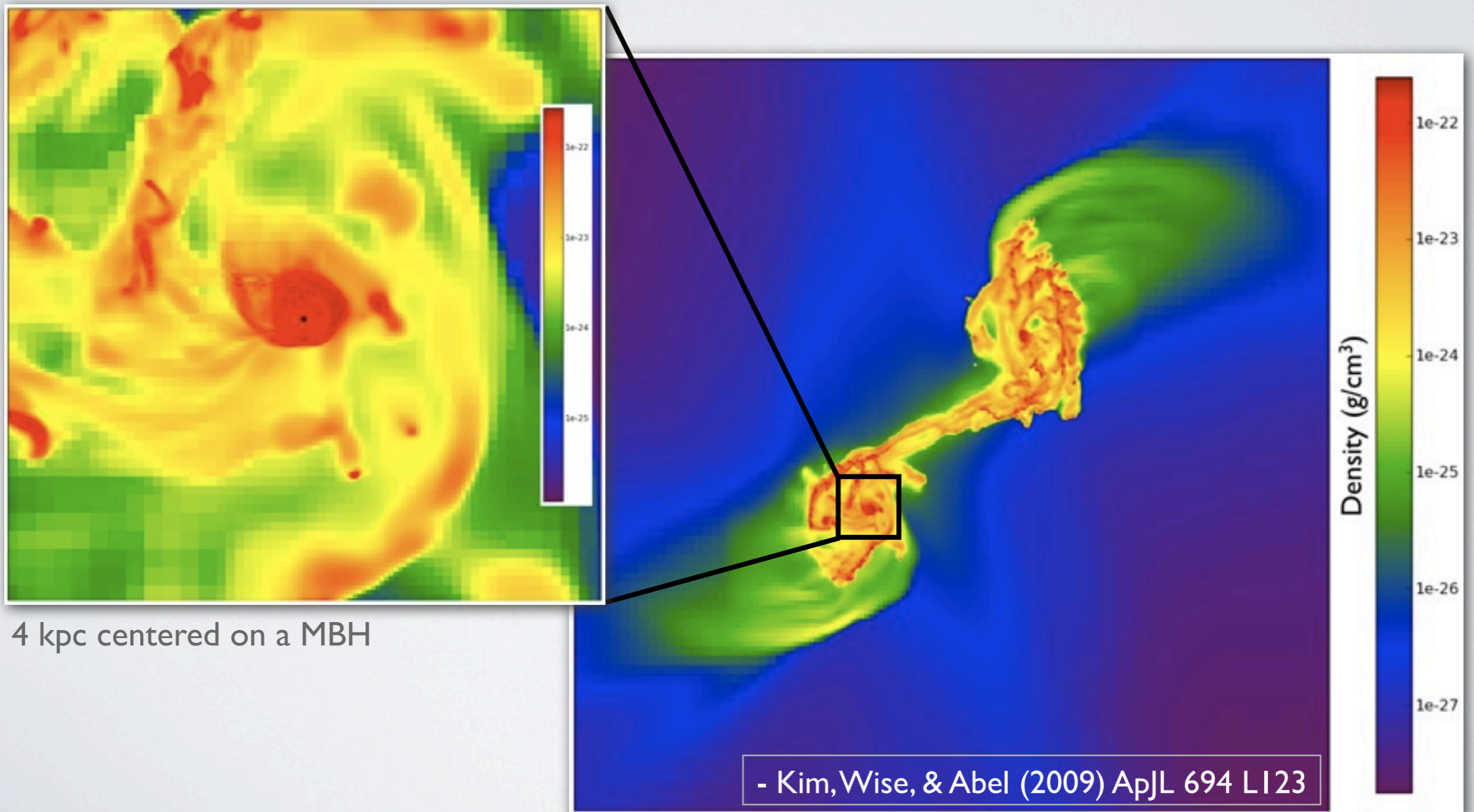


# Galaxy Mergers: Great Laboratory



# Galaxy Mergers

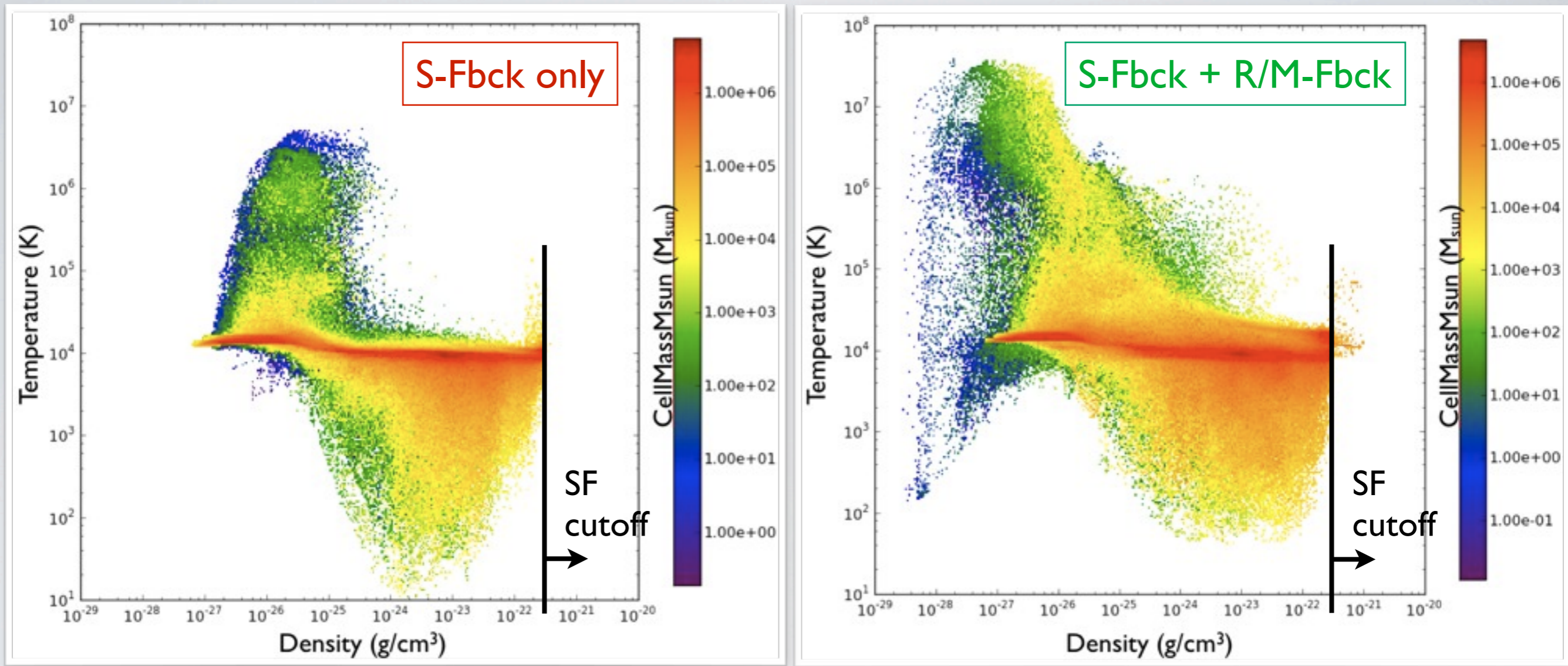
- Two  $2 \times 10^{11} M_{\text{sun}}$  galaxies with embedded  $10^5 M_{\text{sun}}$  MBHs set on a collisional orbit ( $30^\circ$  tilted, initially separated by 80 kpc)



4 kpc centered on a MBH

Density-weighted density proj., 40 kpc, 250 Myrs

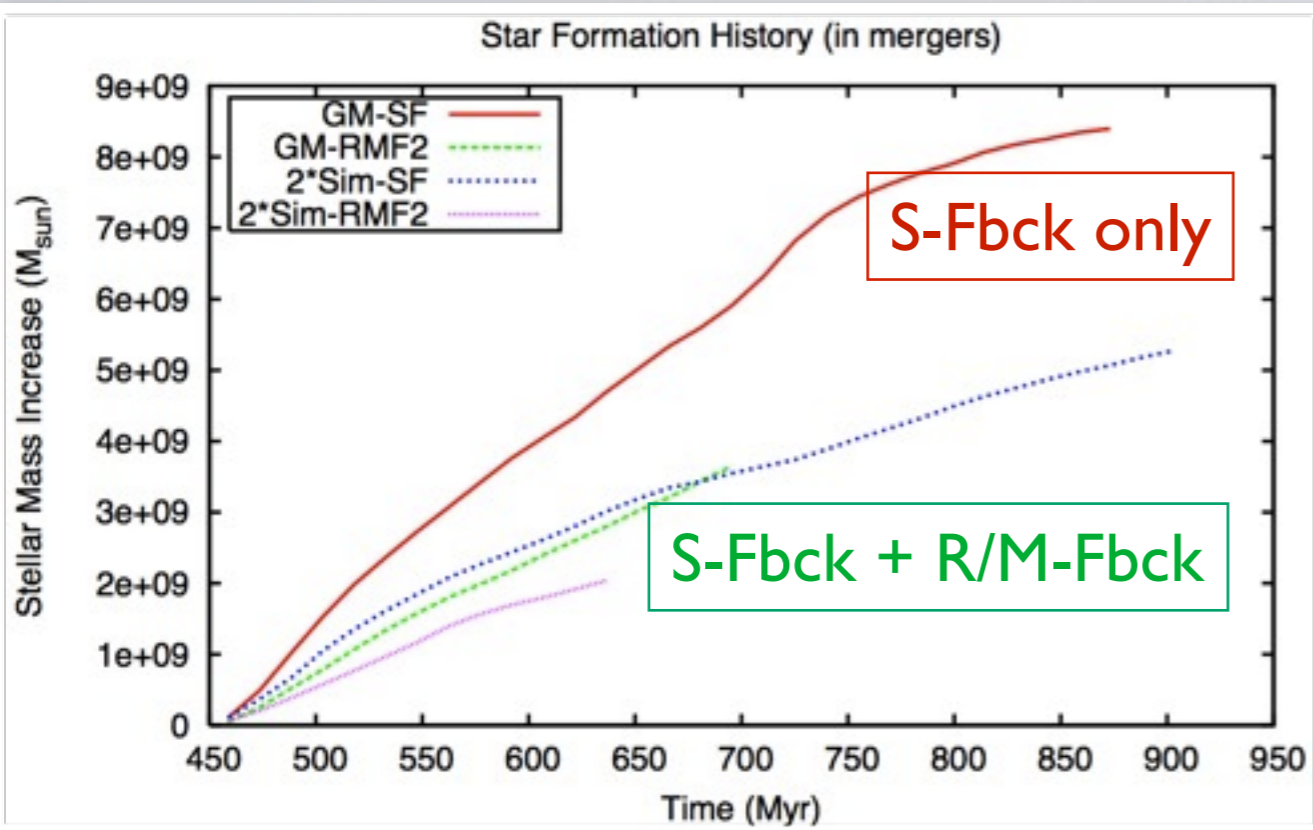
# Density-Temperature PDF



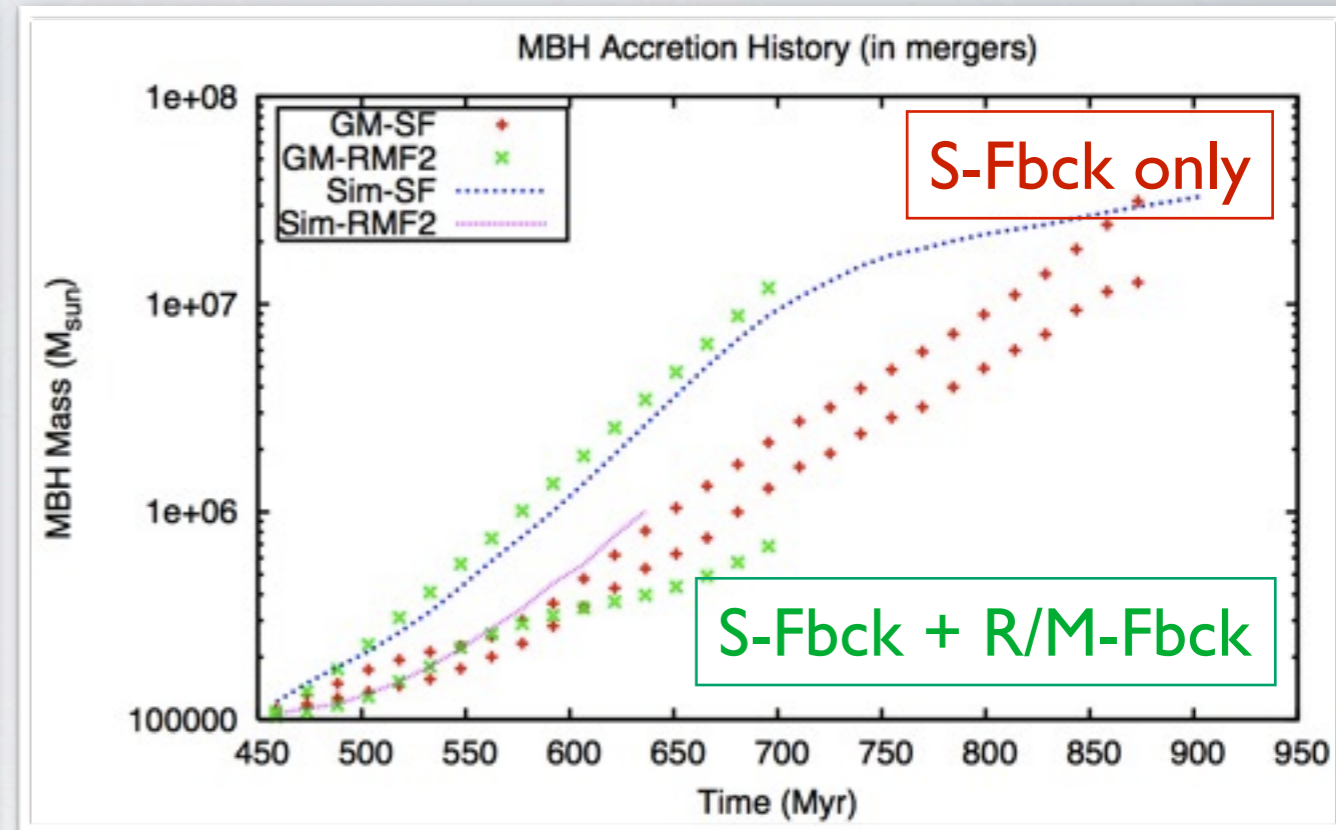
PDF in a 10 kpc sphere centered on one of MBHs

- X-ray radiation significantly **changes** the ISM, and thus SF
- Hot temperature near a MBH prohibits nuclear star formation

# SF and BH Accretion History



SFH (total stellar mass increase)

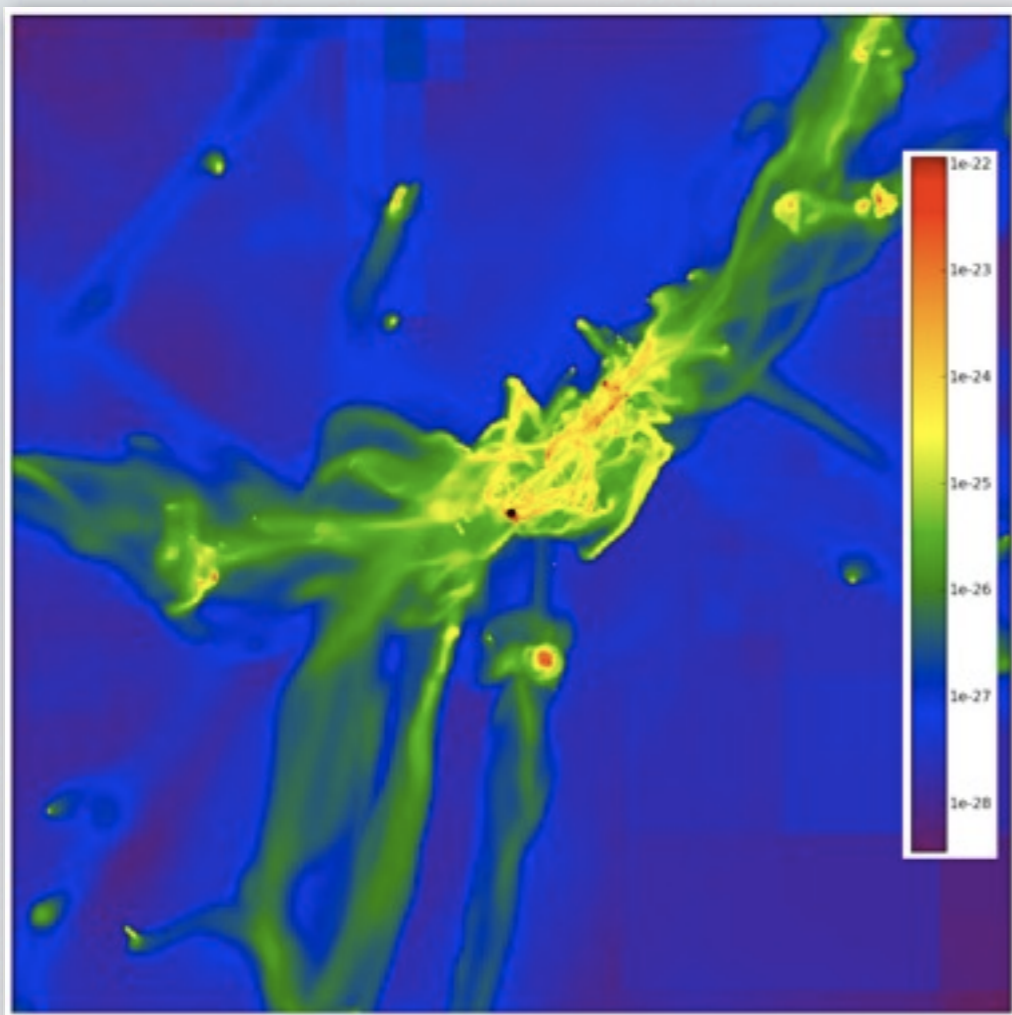


BHAH

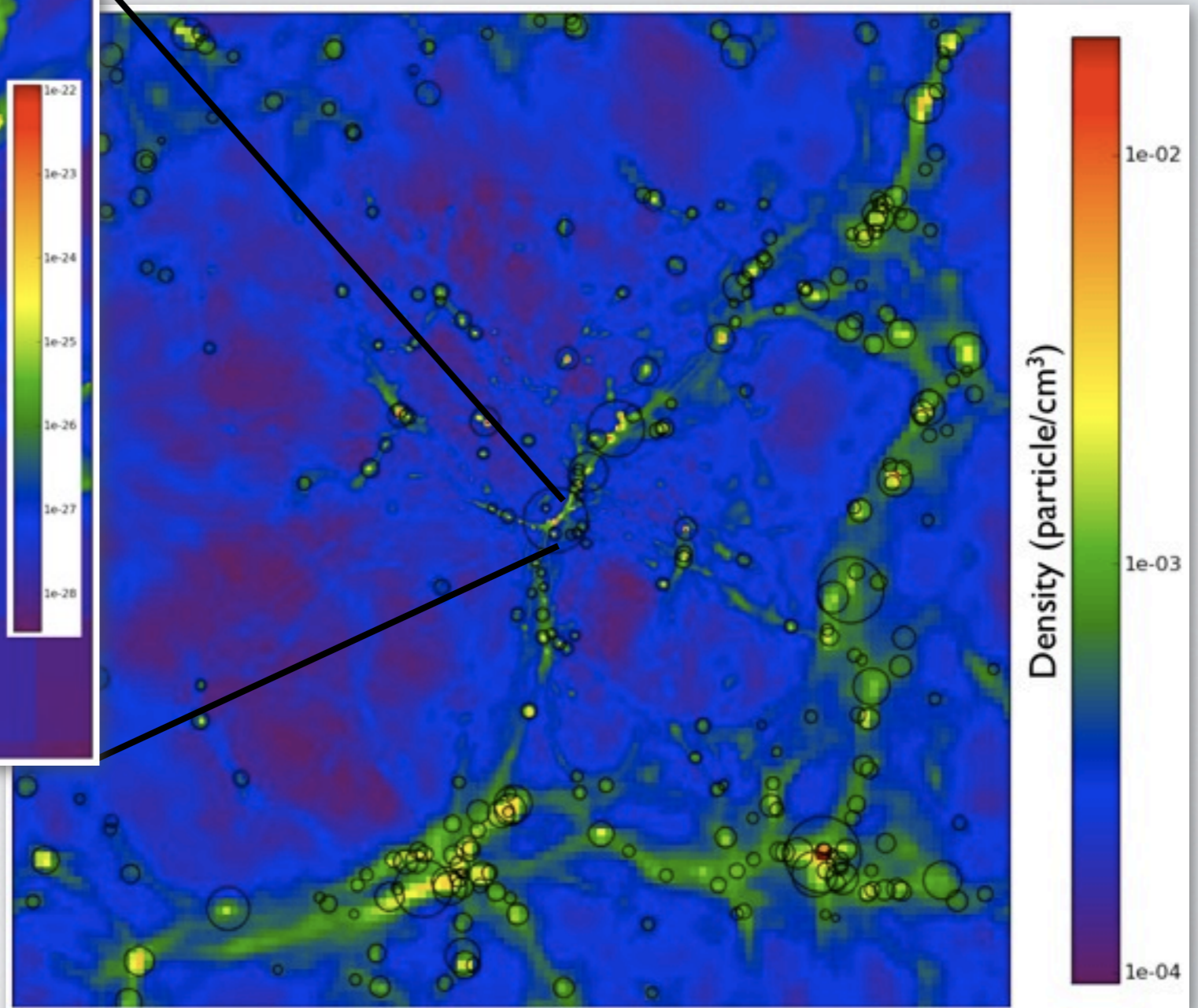
- Star formation rate **suppressed** by soft X-ray radiation from MBH; more to see as two galaxies start to merge
- Jets do not impact much in regulating accretion as they are mostly perpendicular to gas disks

# Cosmological Galaxy Formation at $z=3$

- A  $\sim 10^{12} M_{\text{sun}}$  galaxy selected at  $z=3$  in a low-resolution run  
→ insert a  $10^5 M_{\text{sun}}$  MBH and restart with 15.2 pc resolution

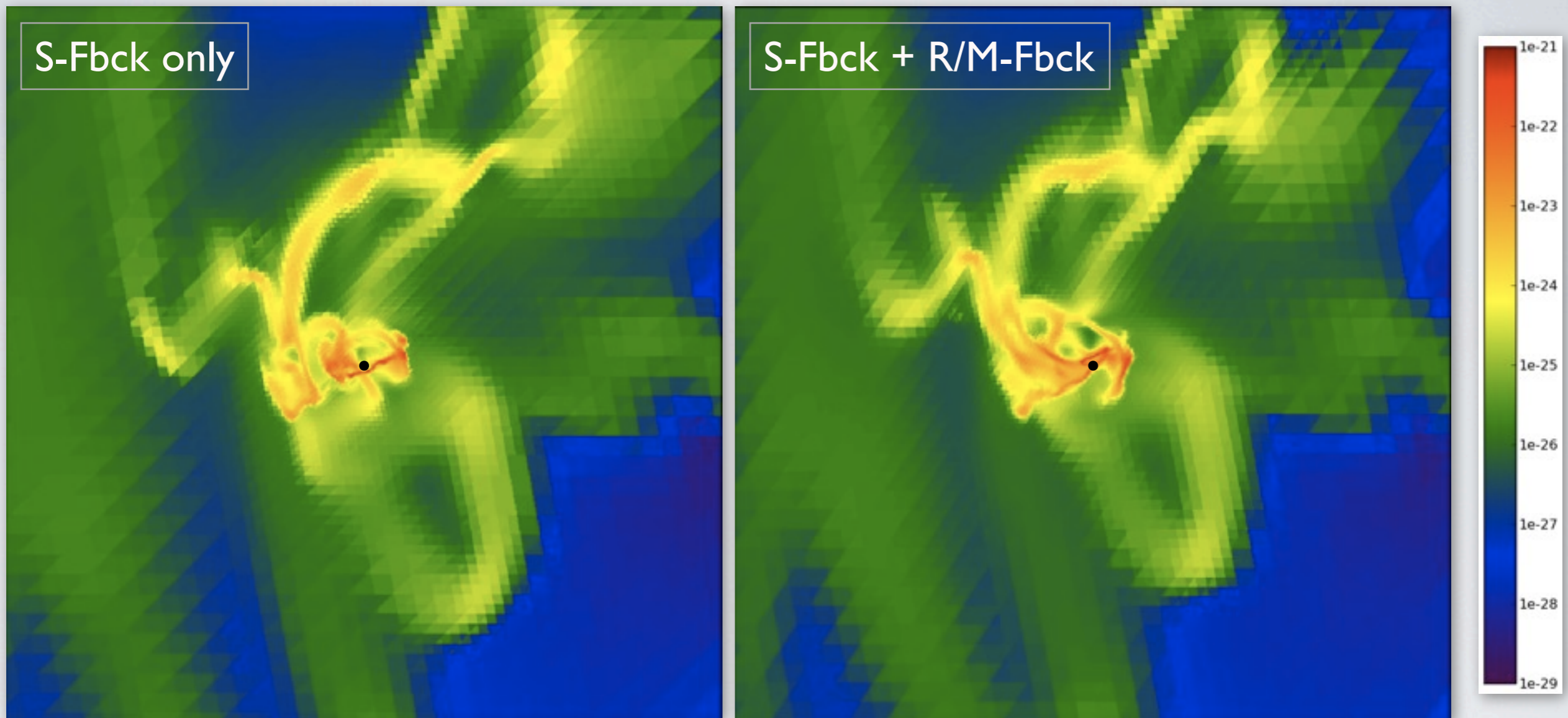


200 kpc centered on a MBH



$z=3$ , Density projection, 16 comoving Mpc

# Density Slice

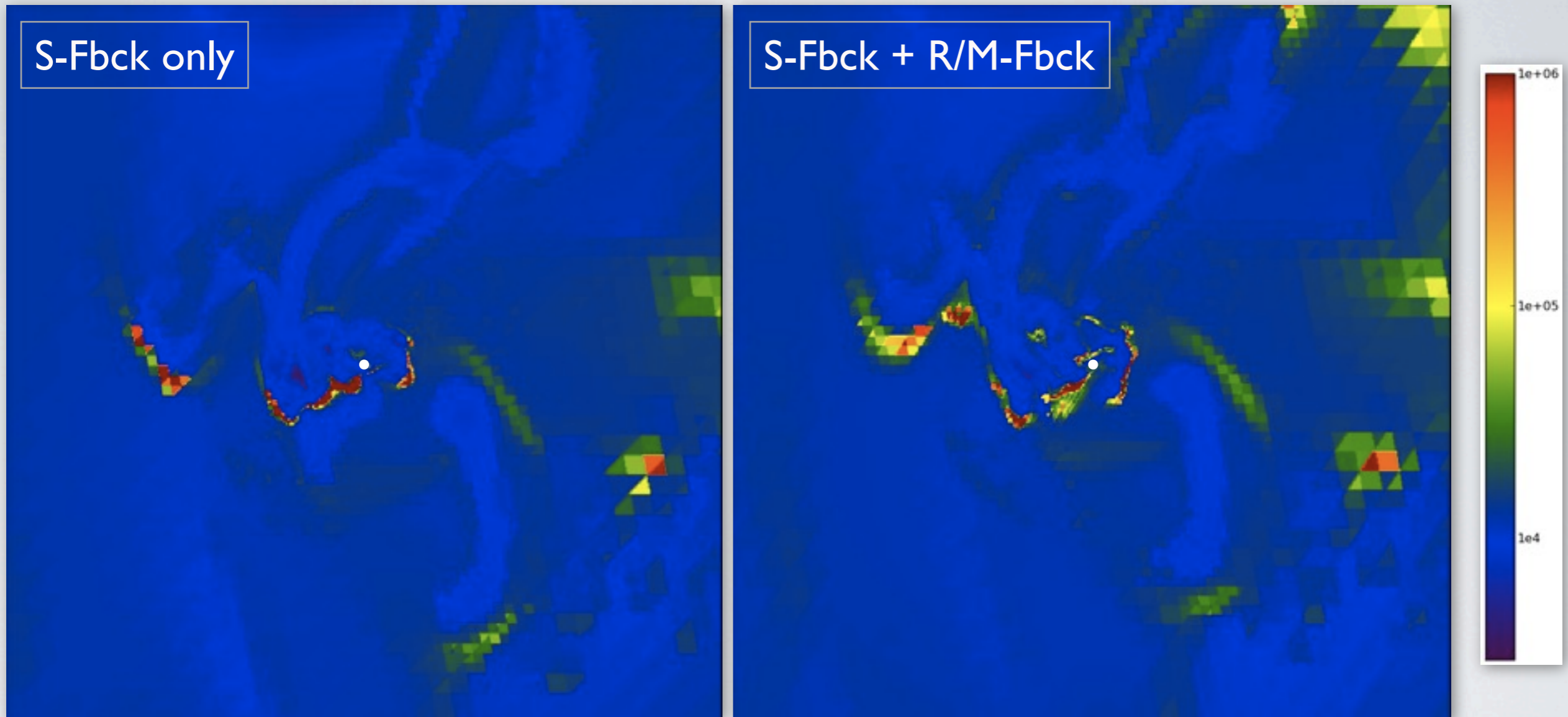


Slice perpendicular to L, 100 Myrs, 20 kpc

- X-ray radiation **heats up** gas clumps and suppresses SF (probably more efficiently because there is no well-defined disk)



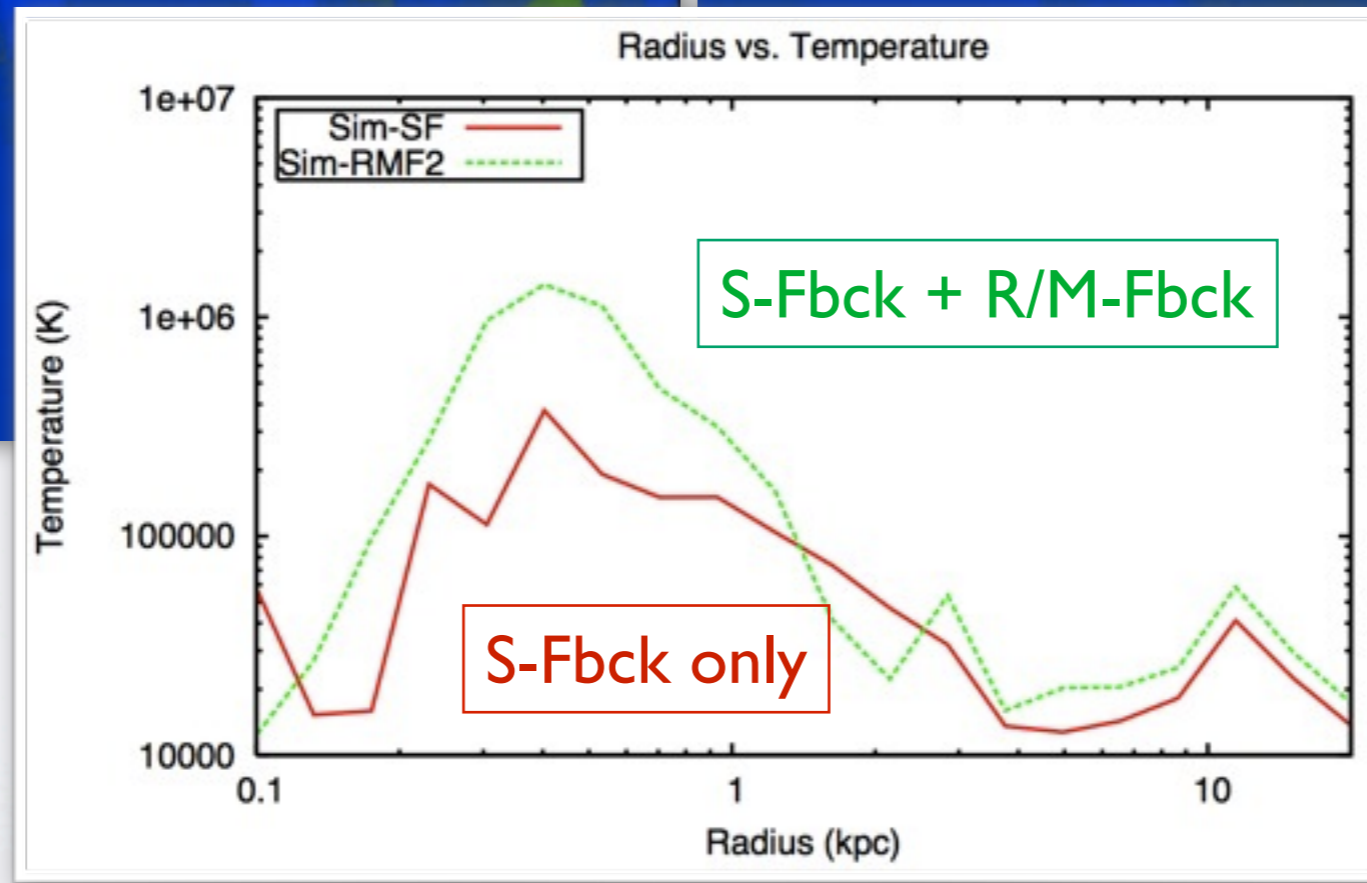
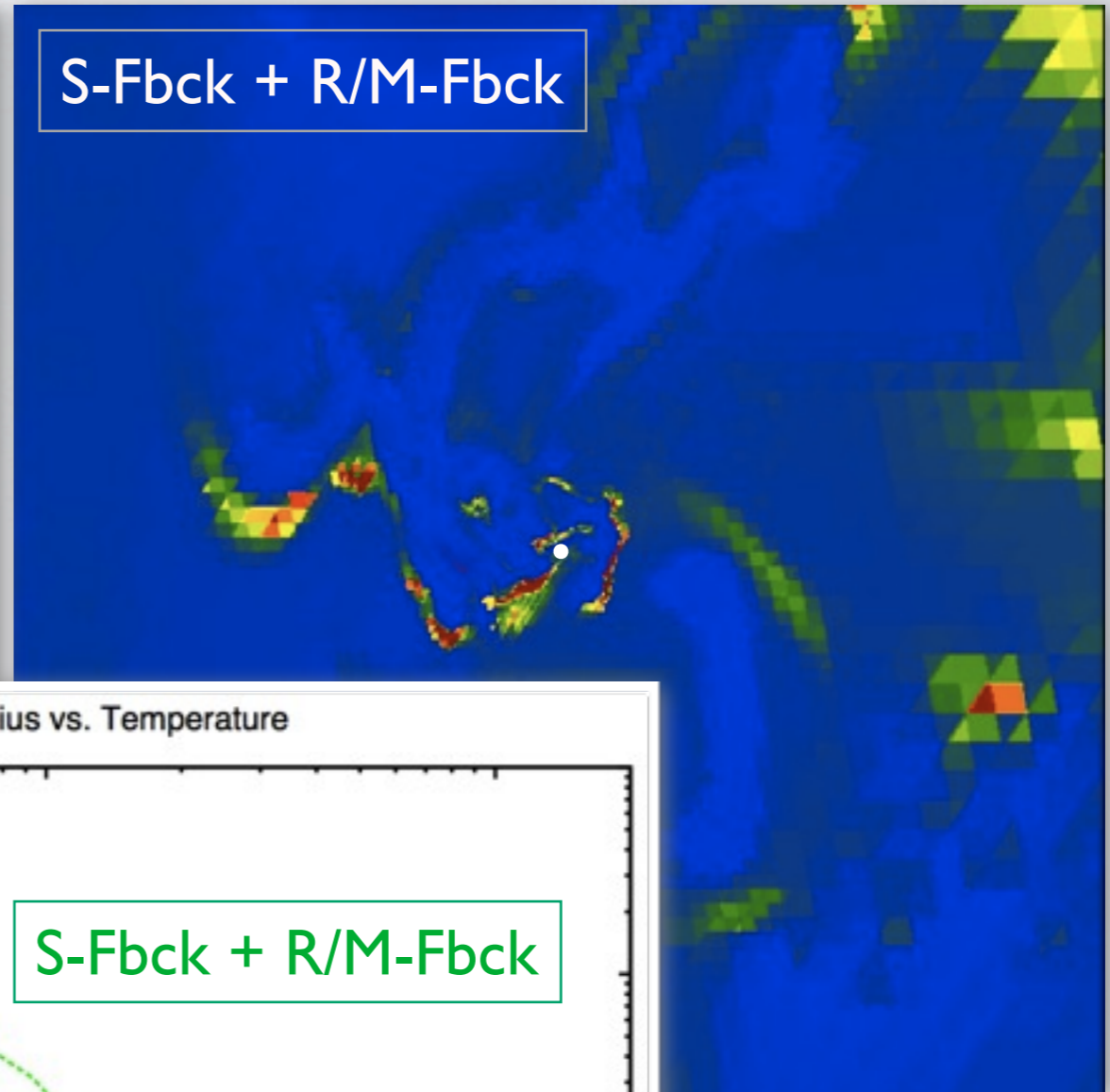
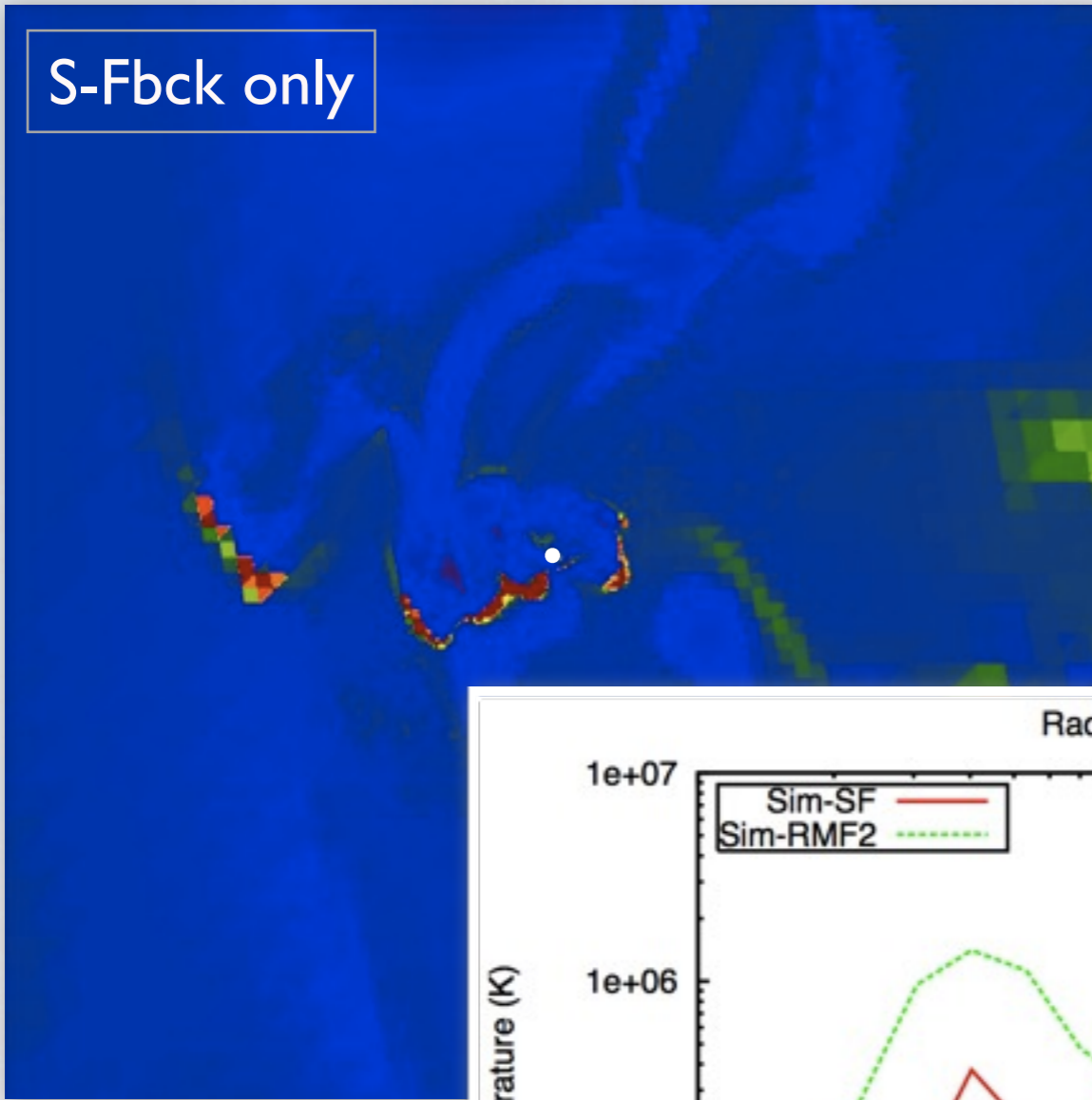
# Temperature Slice



Slice perpendicular to L, 100 Myrs, 20 kpc

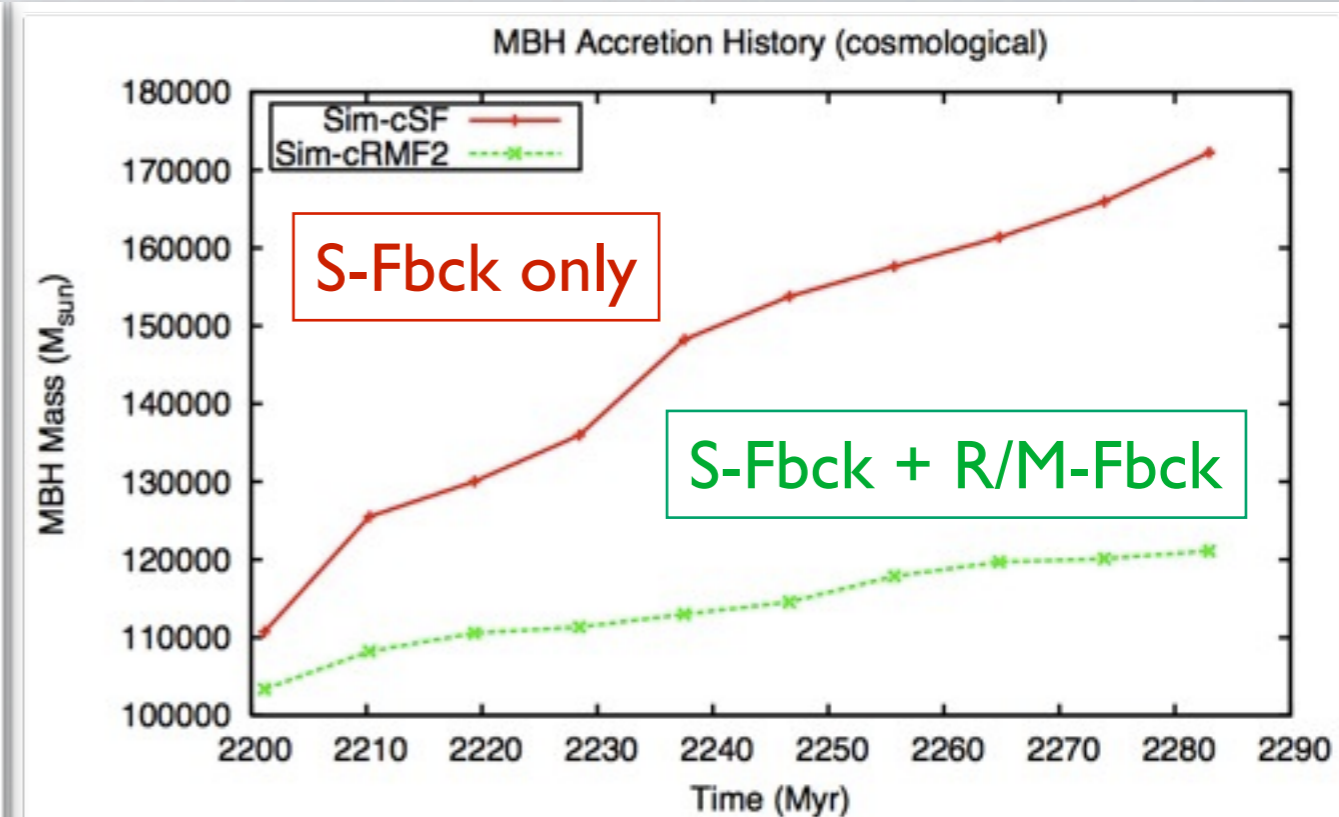
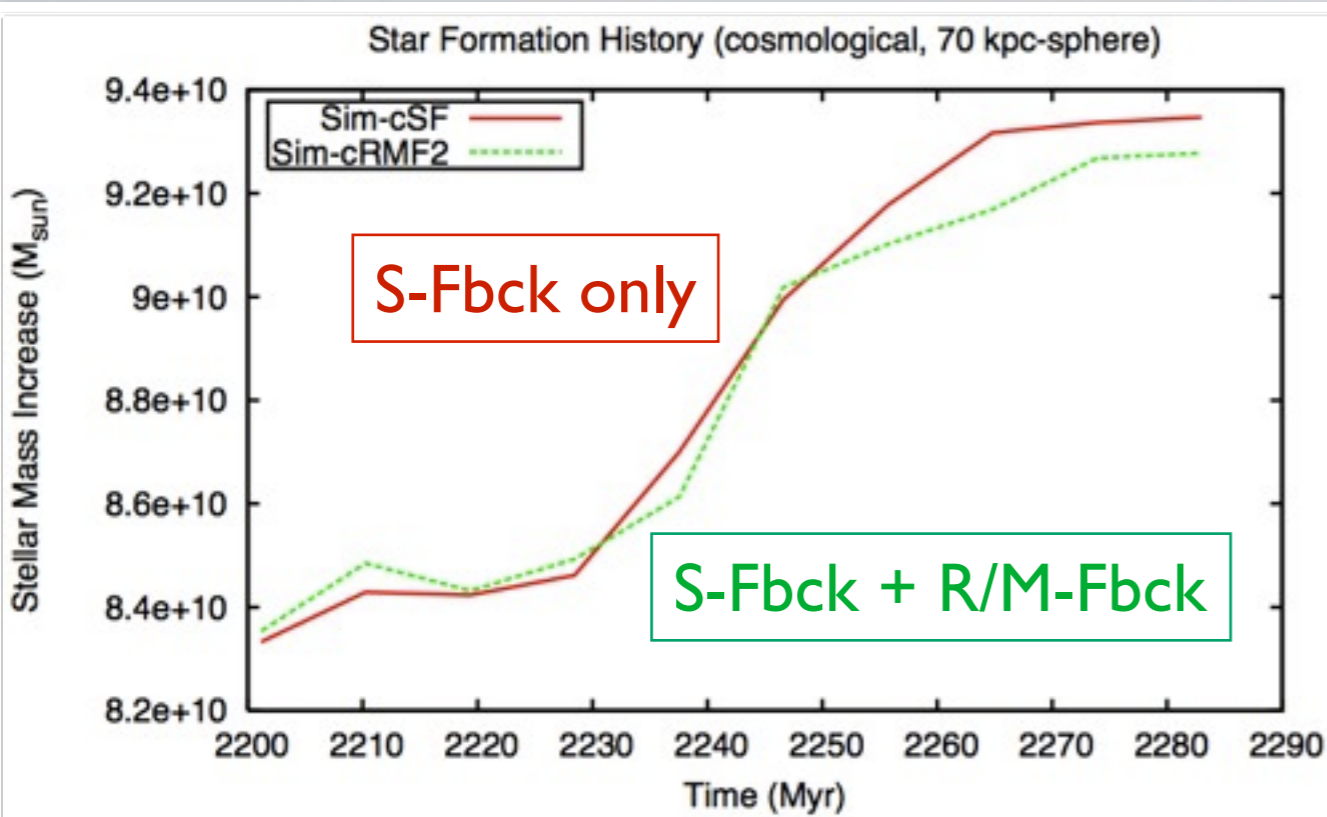
- X-ray radiation **heats up** gas clumps and suppresses SF (probably more efficiently because there is no well-defined disk)

# Temperature Slice



Temperature profile, 20 kpc

# SF and BH Accretion History



SFH (in a 70 kpc sphere centered on the MBH)

BHAH

- Radiation also **regulates** the accretion on to the MBH
- Jets should make more impact with **no well-defined gas disk**

# Conclusion: We are pushing the limit!

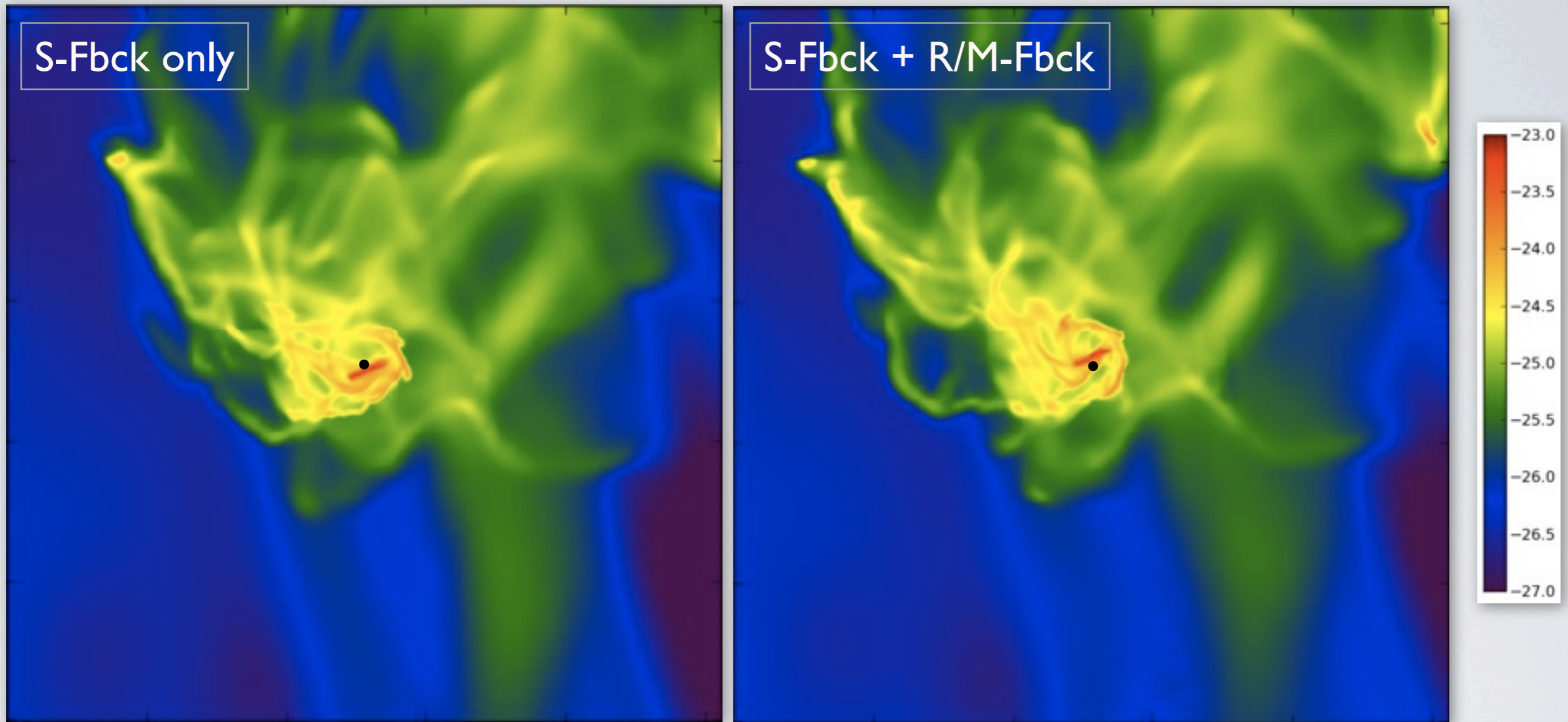
- Various components for understanding the physics of galaxy formation are being pieced together in AMR:
  - Proper treatment of **MC formation & feedback**
  - Proper treatment of **MBH accretion & feedback**
- Preliminary results very encouraging:
  - Stellar and MBH processes in one **self-consistent** framework
  - Radiation from MBH **regulates** SF and its own growth
  - Much more to come!

- Kim, Wise, Alvarez, & Abel (2010) in prep.

- Kim, Wise, & Abel (2009) ApJL 694 L123

# [Supplemental Slides]

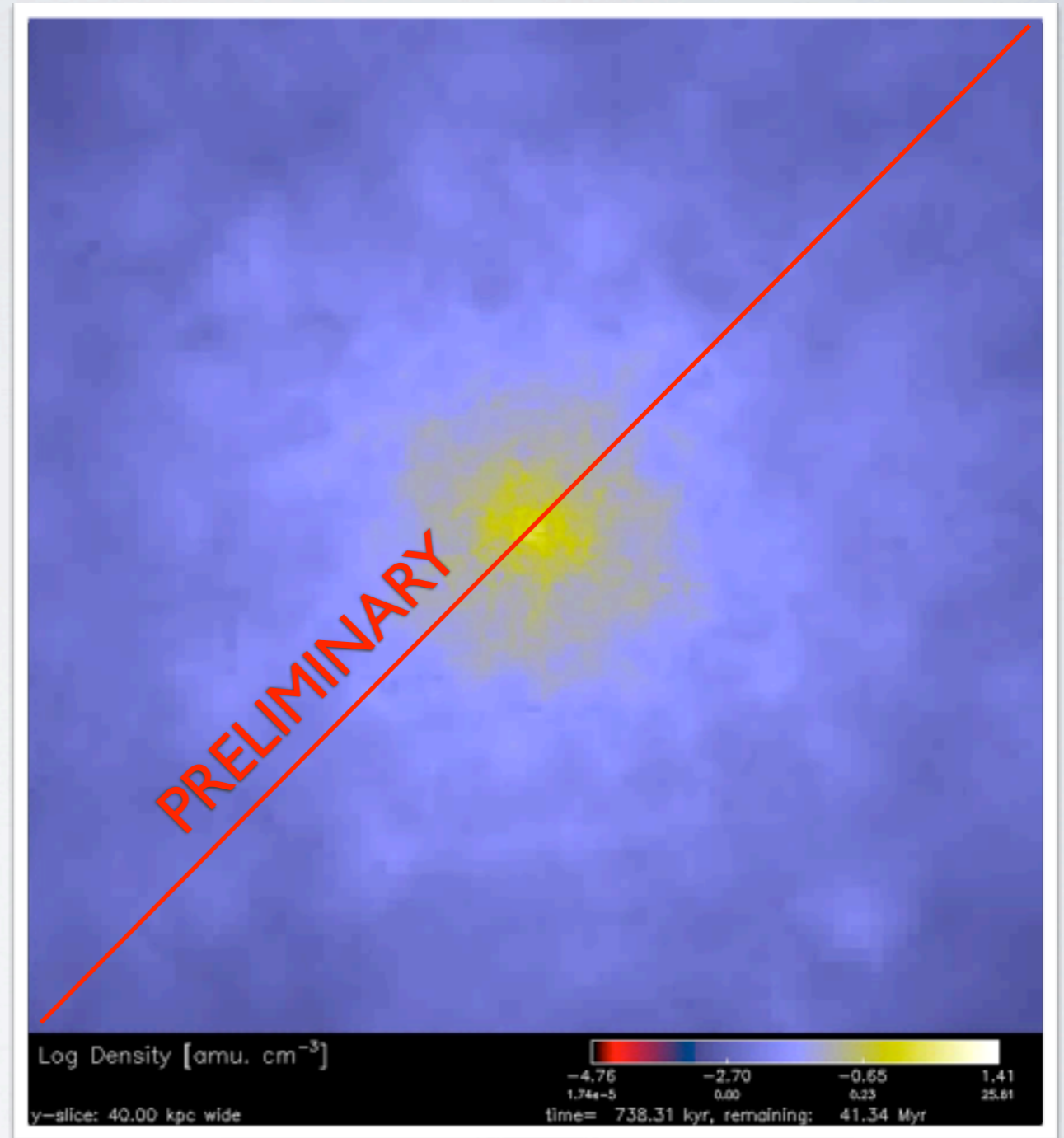
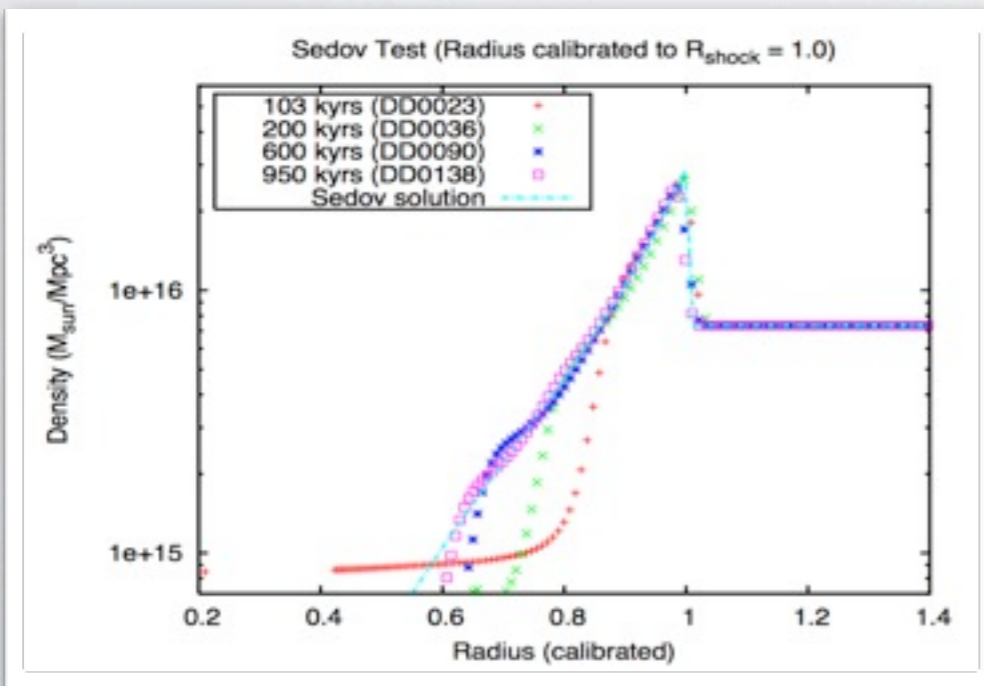
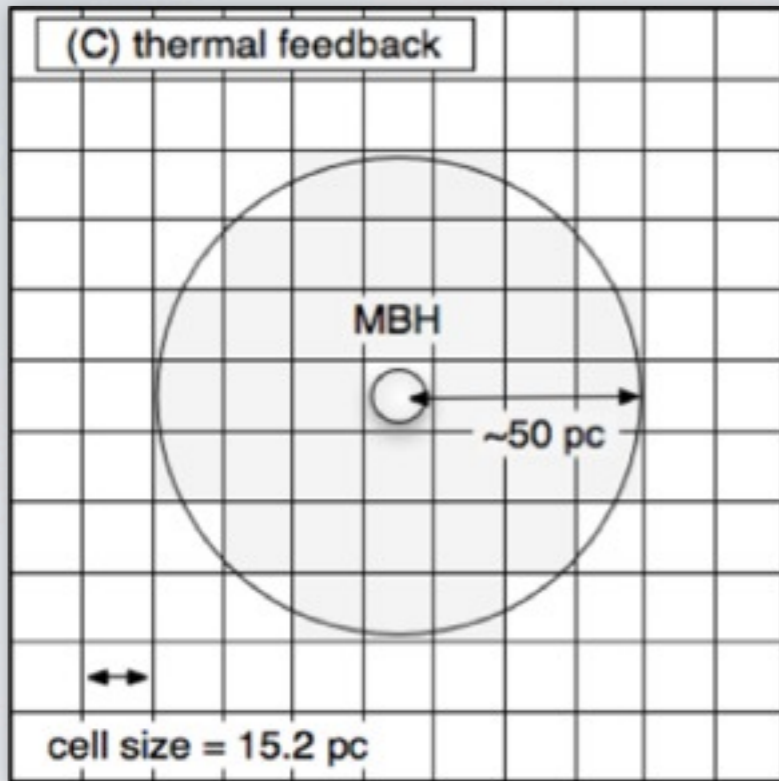
# Density Projection Along L



Projection along L, 100 Myrs, 20 kpc

- Too early to compare morphological differences, yet

# MBH Thermal Feedback



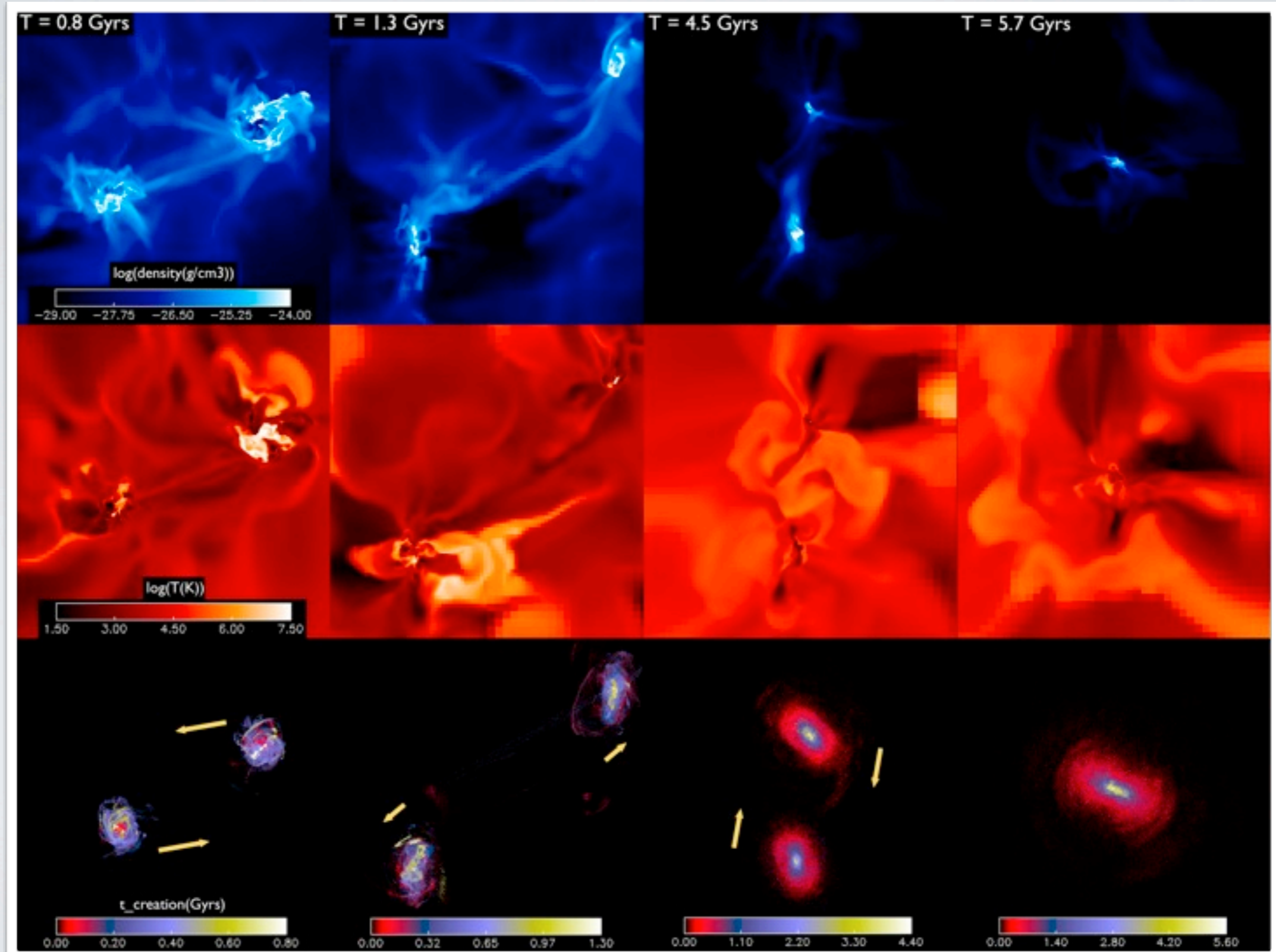
Galaxy = Gas + Stars + MBH + DM, etc.



M51 / HST ACS, "Whirlpool"



# Merger Sequence



- Kim, Wise, & Abel (2009) ApJL 694 L123